

# Performance Assessment of Channel Capacity of Co-operative Communication based System over Dual-hop Asymmetric RF/FSO system



Shyam Baboo Bambiwal, Rajveer Singh Yaduvanshi, Vijay Kumar Pandey

**Abstract:** Cooperative Communication Systems and Relay Selection approaches are recent techniques of wireless communication system that enhance the quality of service (QoS). This research paper probes the execution of the Radio-Frequency and Free Space Optical (RF/FSO) Co-operative system using network of relays. The Co-operative relay system is typically composed of node of a source, the nodes of relays and node of a destination. The source and relay link (S-R link) follow the Generalized-K Fading distribution channel. The link connecting the relay node/device and the destination (R-D link) follows  $\kappa$ - $\mu$  Fading distribution channel. The relay is considered to adopt according to DF i.e Decode and Forward method of relaying and cooperatively assists in transmission to the destination node from the source node. The channel capacity is modelled using PDF (Probability Density Function) for the  $\kappa$ - $\mu$  distribution channel of fading for evaluation of the Dual-hop Asymmetric RF-FSO system. The performance and the analytical expressions of the new system proposed i.e. RF/FSO system were verified and validated using Monte Carlo simulation method.

**Keywords:** Co-operative communication system, Decode-and-Forward relaying, Channel capacity, Generalized-K,  $\kappa$ - $\mu$ , RF/FSO system.

## I. INTRODUCTION

In recent years wireless communications have seen great advancement with technological development. Newer types of networks are being introduced to enhance communication capabilities. Cooperative Communication System is one such newly developed approach based upon broadcast nature of the wireless channel, with same advantage as of MIMO systems. In Cooperative Communication System, active nodes participating in communication, helps to execute the process of communication in distributed fashion [1]. One prime challenging task is to communicate through a wireless

channel, because the medium, in the first place, introduces substantial loss to the signal that is being transmitted. To overcome this, newer communication systems such as Optical Wireless Communication or FSO systems have developed. Main advantages of these newer systems are enhanced capacity and bandwidth when compared to traditional RF based communication systems.

A cooperative network relay system has an “S” as the source, a “D” as the Destination and “N” as the number of relays that operates in flat fading channels. Throughout the cooperative communication system, relay channels establish independent routes between the source (S) and the destination (D) stations. Each wireless user station in co-operative relay communication network is responsible for transmitting data and to participate in communication process as co-operative relay agent [2]. Cooperative communication protocols can be divided into two categories: One as Adaptive Relaying Schemes and other as Fixed Relaying Schemes. In the Fixed relaying protocol, using Amplify and Forward (AF) method which transmits an amplified input version to the “D” destination node. Also in the fixed relaying method using Decode and Forward (DF) relaying protocol, it decodes the received signals first, and then re-encodes them before they are transmitted to the “D” destination node. Any of these two i.e. AF or DF relaying protocol is chosen for the source ‘S’ node and the destination ‘D’ node to establish communication. By using its neighbouring devices as relays, cooperative communication system provides a reliable network form single antenna devices [3]–[6].

In this research paper, mathematical modelling is employed for channel capacity. Performance for of  $\kappa$ - $\mu$  Fading channel in the FSO link of cooperative relay network is evaluated, under DF relaying. The objectives of our work are as under,

- Development of a mathematical modelling for the proposed RF/FSO system and estimate channel capacity.
- To test the arithmetical results obtained and the performance of the system proposed using Monte Carlo simulations.

The remainder of this research paper is organized as follows: Section-II involves review of the literature. Section-III discusses/describe the proposed system, its research methodology and mathematical modelling. Section-IV describes its results and discussion for the proposed system. At last the Section V states our conclusion and scope for future work..

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## II. LITERATURE REVIEW

Palliyembil V (2018) [7] has proposed numerical expressions for outage probability along with channel capacity approach for performance improvement of an RF/FSO system, in which, the source node to relay hop communication noticed Nakagami-m fading whereas the relay node-destination hop noticed M-distribution fading. The alternative useful technique for improving the communication performance of FSO is by making use of multiple transmitting and receiving apertures as well.

Performance Evaluation and comparison between AF and DF relaying schemes for Outrage capacity was done by Chen, X et al. (2015)[8]. The explicit expressions in terms of transmit SNRs were derived. It is found that both methods show the same performance at high source transmission power.

Naurzybayev, G et al. (2018)[9] examined the various wireless powered Dual-hop AF relaying protocols for Ergodic capacity and Outage probability over  $\alpha$ - $\mu$  Fading distribution Channel. The authors proposed analytical expressions in closed-form with respect to the H-functions, and Monte Carlo simulations have confirmed the results.

M. K. Simon & M.-S. Alouini (2005)[10] acquire the outage probability of  $\kappa$ - $\mu$  Fading distribution Channels along with the generalized Marcum Q function. It is assumed the value of  $(m - \mu)$  must not be a positive integer. However, the rest assumed parameters can take any arbitrary value in the fading model of the  $\kappa$ - $\mu$  distribution channel.

Tang, X et al. (2014)[11] carry out an investigation of the performance for multi-hop carried out in RF/FSO systems. Performance for End-to-End Serial transmission (or multi-hop) for optical wireless links have been dealt with previously by several researchers.

The pdf expression for Generalized- $\kappa$  fading channel was derived by Laourine, A et al. (2008)[12]. Results are calculated for expression of the channel capacity by adapting the optimum rate with adaptive power, optimum rate with constant power and channel inversion at a fixed rate. On the other hand, adapting Generalized- $\kappa$  for FSO link is not viable to take recourse to the relaying protocol.

The  $\kappa$ - $\mu$  fading model takes into account a signal which comprises multi-path wave clusters that propagate in a non-homogenous medium. The wave phases that are scattered are assorted randomly in the cluster [13].  $\eta$ - $\mu$  fading distribution model is better suited for non Line of Site propagation (Non-LOS) conditions, which also includes single-sided Gaussian, Nakagami-q (Hoyt), Nakagami-m and Rayleigh fading models as unique case. While on the other hand, for Line of Site(LOS) signal propagation conditions, which included Nakagami (Rice), RayleighNakagami-m, and One-Sided Gaussian fading models, the performance of  $\kappa$ - $\mu$  fading distribution model works well. D. B. da Costa et al., N. Y. Ermolova, K. Peppas et al. and D. Dixit et al. (2008-2012) Studies the execution of different points-to-points cooperative communication systems over the fading channels of  $\kappa$ - $\mu$  and  $\eta$ - $\mu$ .

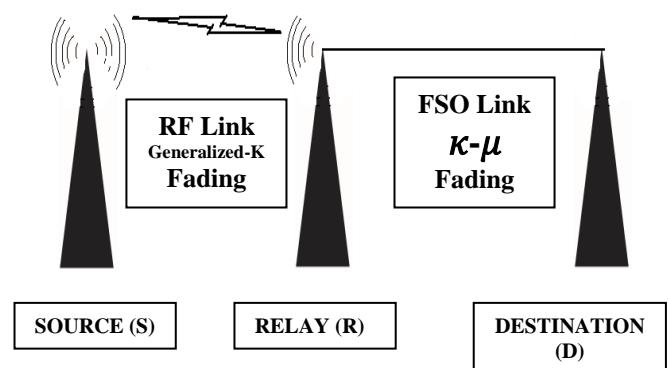
Yacoub, M.D. (2007)[14] dealt with two distributions of fading, namely the distribution channel of  $\eta$ - $\mu$  fading and the distribution channel of fading  $\kappa$ - $\mu$ . It comprised of Rice and Nakagami-m as unique cases, and a border was defined for

the two fading distributions. This paper propounded that,  $\eta$ - $\mu$  fading model accounted for non-LOS communication conditions. Also, the  $\kappa$ - $\mu$  fading model seems to be adjustable in particular. Its notable utility and flexibility are exhibited clearly in this study. Thus we have considered the  $\kappa$ - $\mu$  fading model in our study for the FSO link of co-operative communication system under Dual-hop asymmetric DF relaying protocol.

## III. METHODOLOGY

With context to co-operative wireless communication systems, Dual-hop relaying is highly adapted as spatial diversity presented by it. It can extend the coverage area efficiently under potentially severe condition of channel fading. RF connections are usually used in most relaying systems to establish complete end-to-end communication.

However, the scarceness of conventional dual-hop RF/RF communication which are licensed-spectrum resources along with the ever-increasing requirements of high-speed communication systems and need for more multi-user accessibility are some of the most critical constraints, FSO cooperative communication systems have incurred considerable research curiosity because of its enviable characteristics. As shown in Figure1 the proposed cooperative Relay Network Model consists of an ‘‘S’’ as the source node, an ‘‘R’’ as relay agent/node, and ‘‘D’’ as the destination/target node. Dual-hop Asymmetric FSO/RF systems are considered, where in the first hop, data shall be forwarded from the Source ‘S’ to the Relay ‘R’, and in other/next second hop, the data is released from the Relay ‘R’ to the Destination ‘D’. For the Source to the Relay, the RF link is set up (S-R link), and the FSO link is used from the Relay Agent to the Destination (RD link).The S-R link follows Generalized-K fading distribution channel, while the link R-D follows  $\kappa$ - $\mu$  fading channel. The  $\kappa$ - $\mu$  fading distribution renders a general type multipath model for the Line of Sight (LOS) propagation scenario, which is then controlled by the two shaping parameters  $\kappa$  and  $\mu$  [21].



**Figure 1: RF-FSO system Model**

### A. RF (S-R) link

The RF link follows Generalized- $\kappa$  fading distribution. The Generalized- $\kappa$  model combines Nakagami-m multipath fading in the S-R link. The PDF of Generalized- $\kappa$  fading channel in terms of instantaneous SNR can be expressed as given by [22]

$$p(\gamma_{sr}) = \frac{\alpha^{\beta+1}}{2^{\beta}\Gamma(m)\Gamma(\kappa)} \gamma_{sr}^{\frac{\beta-1}{2}} K_{\alpha}(a\sqrt{\gamma_{sr}}) \quad (1)$$

Here  $a = \sqrt{\frac{4\kappa m}{\bar{\gamma}}}$  and other mentioned symbols in the formula the ‘ $\kappa$ ’ and the ‘ $m$ ’ are the shaping/molding parameters of Generalized- $\kappa$  combined with the Bessel function of order  $\alpha$  is defined as the Nakagami- $m$  channel distribution. Here  $\alpha = \kappa - m$ , and  $\beta = \kappa + m - 1$ . Also  $K_{\alpha}(\bullet)$  exists as known Bessel function of order  $\alpha$ . Here  $\alpha$  expression is in terms of  $\bar{\gamma}$  which is the average value of the SNR.

**B. FSO (R-D) link**

The FSO communication systems have multiple merits such as inexpensive execution of installation, economical working costs because of license free spectrum, simple deployment, high data rate and immunity to interference. The FSO link of the proposed relay network follows  $\kappa$ - $\mu$  fading distribution. Rice that is Nakagami- $n$ , Nakagami- $m$ , one-sided Gaussian, and Rayleigh distributions are unique cases of the proposed fading model [18]. The relation between the power of the main components and the wave power that are unevenly distributed is represented by  $\kappa$ , and  $\mu$  is the non-negative natural real number. The PDF of  $\kappa$ - $\mu$  channel in R-D link is expressed as

$$p(\gamma_{rd}) = \left\{ I_{\mu-1} \left( 2\mu\sqrt{\kappa(1+\kappa)\Omega^{-1}\gamma_{rd}} \right) \right\} \times \frac{\mu(1+\kappa)^{\frac{\mu+1}{2}} \gamma_{rd}^{\frac{\mu-1}{2}}}{\kappa^{\frac{\mu-1}{2}} e^{\mu\kappa\Omega} \frac{\mu+1}{2}} e^{-\frac{\mu(1+\kappa)}{\Omega} \gamma_{rd}} \quad (2)$$

Where  $\Omega = \mathbb{E}[\gamma_{rd}^2]$ , is the expectation operator. For unique cases, this  $\kappa$ - $\mu$  fading channel contains Rice ( $\kappa = K$ ,  $\mu = 1$ ), Nakagami- $m$  ( $\kappa = 0$ ,  $\mu = m$ ) and one-sided Gaussian distribution ( $\kappa = 0$ ,  $\mu = 0.5$ ).

**C. Assessment of capacity of Channel.**

Assessment of capacity of Channel is vital performance of wireless cooperative communication system. The extensive demand for wireless communication makes it imminent to ascertain the capacity limits of fading channels. The channel capacity serves as the higher limit of the data speed for reliable communication over noisy channel, and is defined in the paper in terms of outage probability. For deriving the expression of channel capacity, Outage probability formula is employed. And the formula for outage probability of  $\kappa$ - $\mu$  fading distribution is expressed in Equation (3)

$$P_{out}^{\kappa,\mu} = \sum_{m=0}^N \binom{N}{m} Q_{\mu}^m(a,b) \times [1 - Q_{\mu}(a,b)]^{N-m} \times [1 - Q_{(m+1)\mu}(c,b)] \quad (3)$$

Where  $a = \sqrt{2\mu\kappa}$  ;  $b = \sqrt{2\mu(1+\kappa)\Omega^{-1}\Delta}$  ;  
 $c = \sqrt{2(m+1)\mu\kappa}$ ;

Also here  $Q$  is the generalized Marcum  $Q$  function that calculates the Marcum  $Q$  of 2 non-negative real numbers ‘ $a$ ’ and ‘ $b$ ’. This generalized Marcum  $Q$  function is a built in tool function like in MATLAB, MATHEMATICA etc. and is

expressed as follows:

$$Q(a,b) = \int_b^{\infty} x \exp\left(-\frac{x^2+a^2}{2}\right) I_0(ax) dx \quad (4)$$

Here  $I_0$  = modified Bessel function of the first kind with zero order.

Channel capacity for R-D link can be calculated using following formula for  $\kappa$ - $\mu$  fading channel distribution is given by

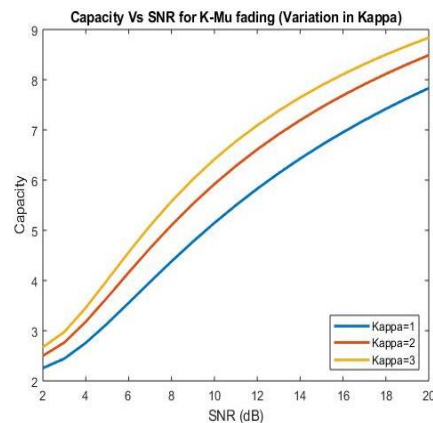
$$C = (1 - P_{out}^{\kappa,\mu}) B \log_2(1 + \gamma) \quad (5)$$

Therefore, the closed-form explicit channel capacity expression for the  $\kappa$ - $\mu$  fading channel distribution in FSO link and can be obtained by substituting Equation (3) in (5),

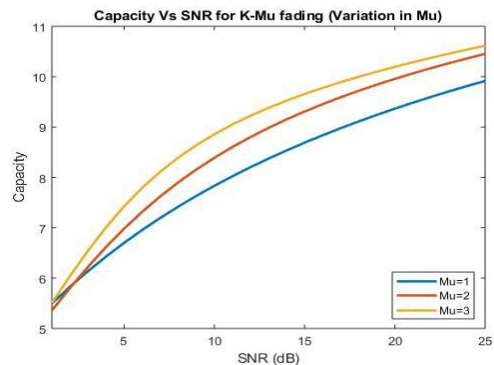
$$C = \left( 1 - \sum_{m=0}^N \binom{N}{m} Q_{\mu}^m(a,b) \times [1 - Q_{\mu}(a,b)]^{N-m} \right) \times [1 - Q_{(m+1)\mu}(c,b)] B \log_2(1 + \gamma) \quad (6)$$

**IV. RESULTS AND DISCUSSION**

After procuring the expression for the channel capacity, Monte Carlo simulation method is used for verifying and validating the numerical expressions using MATLAB software. Channel capacity was plotted against SNR values for various  $\kappa$  values ( $\kappa=1$ ,  $\kappa=2$ ,  $\kappa=3$ ) as shown in the Figure 2. It is inferred from the graph that for higher  $\kappa$  values, the channel capacity shows improved results.



**Figure 2: Channel capacity for different  $\kappa$  values**  
Channel capacity is plotted against SNR values for various  $\mu$  values ( $\mu=1$ ,  $\mu=2$ ,  $\mu=3$ ) as depicted in the Figure 3. It is deduced from the graph that, with the rise in the  $\mu$  values, there is a significant improvement in the channel capacity.



**Figure 3: Channel capacity for different  $\mu$  values**



## V. CONCLUSION

The Channel capacity of co-operative relay system using DF relaying protocol is researched in  $\kappa$ - $\mu$  fading channel in the FSO link. Computationally efficient closed-form mathematical derivation for the capacity of noisy channel in terms of outage probability is delineated in the paper. Mathematical results have been drawn using MATLAB software to explain the enhancement in the capacity of the channel with respect to the escalation in the  $\kappa$  and  $\mu$  values of the  $\kappa$ - $\mu$  fading channel of R-D link of co-operative communication system. Using the findings obtained from this research, evaluation of the performance of channel communication can be undertaken in the future for the betterment of field of co-operative relaying communication system.

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