



Scheduling of Machines and AGVs Simultaneously in FMS through Hybrid Teaching Learning Based Optimization Algorithm

Kanakavalli Prakash Babu, Vommi Vijaya Babu, Medikundu Nageswara Rao

Abstract: *The most complex problem in FMS is scheduling task, due to this complexity it has created interest among many researchers. Even though FMS scheduling problem was considered earlier, material handling systems like (AGVs) scheduling was not done effectively. As transportation times cannot be neglected in an FMS, a carefully managed and designed material handling system is important in achieving the required integration in flexible manufacturing environment. Hence there is a need for scheduling both the machines and material handling system simultaneously for the successful implementation of an FMS, which makes the scheduling of FMS more complex. Metaheuristic Algorithms are mostly received by the researchers, because of their capability to tackle more complex problems. Hybridization of the metaheuristics may further improve their performance. In the present work a new hybrid metaheuristic Teaching Learning based optimization (HTLBO) is proposed to solve simultaneous scheduling problems.*

Keywords : AGVs, FMS, Operational Completion Time (makespan), Metaheuristic algorithms, , NP-hard problems

I. INTRODUCTION

Producing wide variety of parts in low to mid volume quantities at a low cost while maintaining a good quality in end items is one of the characteristic of Flexible Manufacturing System (FMS). FMS executed number of benefits in terms of cost reduction- increased machine utilization - reduced work-in-process levels- etc. However- there are many problems encountered during the life cycle of an FMS and these are classified into: design- planning- scheduling- and controlling. In particular- the scheduling task and control problem during the manufacturing operation are of importance owing to the dynamic nature of the FMS in respect of flexible parts- tools- assignments. In FMS not only sequencing of jobs on machines

But also the routing of the jobs through the system must be taken into consideration. Apart from the machines- other resources in the system like Automated Guided Vehicle (AGV) and Automated Storage/Retrieval System (AS/RS) must be considered The AGVs effectiveness depends on vehicle management system.

II. LITERATURE REVIEW

A. Simultaneous scheduling in FMS

In simultaneous scheduling- the real time as well as the off-line scheduling is taken into account. Bilge and Ulusoy [1] exploited the interactions between the machine and AGVs scheduling simultaneously. The material transfer between machines is done by a number of identical AGVs which are not allowed to return to the load/unload station after each delivery. Abdelmaguid et al.[2] suggested a hybrid GA for minimizing the makespan. The algorithm is implemented to a set of 82 test problems- which was constructed by other researchers- and the comparison of the results indicates the superior performance with the developed coding. Reddy and Rao [3] studied the simultaneous scheduling problem with makespan- mean flow time and mean tardiness as an criterion. The proposed hybrid GA for FMS scheduling problems yielded better results when compared to other algorithms. Gnanavelbabu et al. [4] examined simultaneous scheduling in FMS using DE with makespan minimization. Anandaraman et al. [5] presented a solution for the simultaneous scheduling problem by evolutionary approach in FMS with vehicles and robots. The scheduling optimization is carried out using metaheuristic algorithm. The algorithms are implemented for bench mark problems taken from the literature and the comparison is also done. Nouri et al. [6] introduced the clustered holonic multiagent model using metaheuristic for simultaneous scheduling of machines and transport robot in FMS. Computational results are presented using three sets of benchmark instances in the literature. New upper bounds are found- showing the effectiveness of the presented approach. Md Kamal et al. [7] Flexible Job Shop Scheduling Problem (FJSSP) is an extension of the classical Job Shop Scheduling Problem (JSSP).

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Keeping in view this aspect- this article presents a comprehensive literature review of the FJSSPs solved using the GA. The survey is further extended by the inclusion of the hybrid GA (HGA).Nageswara rao et al [8].

III. SIMULTANEOUS SCHEDULING PROBLEMS IN FMS

A. Problem structure

Bilge and Ulusoy (1995) proposed a numerical example for simultaneous scheduling of machines and AGVs in FMS environment which includes four layouts- ten jobsets process times and travel time data. This data is considered as input in the present work.

B. Objective function

Operation completion time = $O_{ij} = T_{ij} + P_{ij}$
 T_{ij} = Traveling time for j^{th} operation and i^{th} job
 P_{ij} = operation processing time

C. Optimization parameters considered

Population Size = Double the no of operations
 Iterations completed = 1000

D. Vehicle Assignment Procedure

It is required to schedule both material handling system and machines at a time in this problem. To obtain the makespan value for a given sequence of operations the following procedural steps are implemented.

- Step 1: Consider the machine number (M.No) of the given sequence for the job.
- Step 2: Select the AGV
- Step 3: Identify the vehicle previous location (VPL)- previous operation machine number (POMN)- vehicle ready time (VRT) and previous operation completion time (POCT)
- Step 4: Calculate vehicle empty trip time (VET) using $VET = VRT + VPL \text{ to POMN}$.
- Step 5: Select the maximum among POCT and VET.
- Step 6: Obtaining the total travel time of vehicle (TT) using $TT = VET + POMN \text{ to M.No}$.
- Step 7: Find the machine readiness time (MRT).
- Step 8: Identify the maximum among TT and MRT.
- Step 9: Maximum time (from step 8) is added to process time to get the operational completion time.
- Step 10: Repeated the steps from 2 to 9 for all other operations.
- Step 11: Identify the maximum operational completion time- which represents the possible completion time (makespan) of given job set.

IV. TEACHING LEARNING BASED OPTIMIZATION

Teaching Learning Based Optimization (TLBO) algorithm is proposed by Rao et al. (2011). It comprises two phases Teacher phase that is gaining knowledge through teacher and Learner phase gaining knowledge through learner to learner interaction. The steps involved in the algorithm are shown in the flow chart (Figure.1).

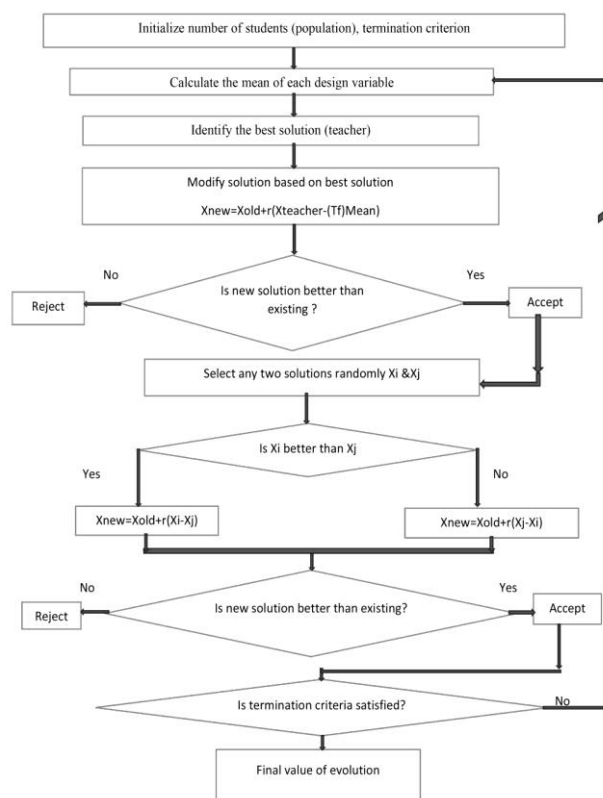


Figure.1: Flow chart for TLBO algorithm

A. Hybrid Algorithms

Since mixing of any two algorithms yields superior results, TLBO is amalgamated with Sheep Flock Heredity Algorithm.

B. Sheep Flock Heredity Algorithm

Sheep Flock Heredity Algorithm (SFHA) was developed by Hyunchul Kim (2001). This algorithm is based on the genetic inheritance.

The steps involved in SFHA are given below:

- Step 1: Generate Initial population randomly.
- Step 2: The desired optimization fitness is evaluated for each chromosome.
- Step 3: Sub chromosome level crossover and mutation must be done
- Step 4: Do the chromosome level crossover and mutation process by selecting the best chromosome from the population.
- Step 5: Calculate the fitness function for each chromosome in the population. Then do the sorting function.
- Step 6: After sorting the strings, to do the editing of the chromosomes in the population after the mutation process.
- Step 7: After editing the chromosomes in the population the new population has to undergo next iteration until termination criterion is reached.

C. Hybrid Teaching Learning Based Optimization

- Step 1: Consider the job set
- Step 2: For the job set implement TLBO as explained in Section. IV to get the sequence of operation.

Step 3: After getting the sequence of operation for each iteration, crossover and mutation concepts are to be implemented.

D. Algorithm to Optimal Scheduling Problem

For illustration of HTLBO, Job set 9 and Layout 1 are taken into consideration. Data related to jobset 9 is shown in Table.I. HTLBO algorithm computes the effect of the influence of a teacher on the output of learners in a class and receptor editing for different jobs and the sequences are obtained based on results or grades.

The HTLBO algorithm is illustrated below for job set 9:

Step 1: Considering the job set

In HTLBO for the operation in a job set numbers are assigned serially.

Step 2: Initializing the optimization parameters.

Teaching Factor, (TF) = 1 or 2, Random number = 0 to 1

Step 3: Initial population is generated randomly by following precedence relation, these are presented in table 1. The makespan for each sequence is calculated to implement the steps discussed in article III section.D to identify the maximum operational completion time (makespan) for each sequence.

From the above table it can be interpreted that in 1st sequence, number '8' represents 1st operation on the job no 3 and similarly number '14' represents the 1st operation on job no 5. Similarly number '17' represents 4th operation on job no 5 and so on.

Step 4: Teacher phase.

A good teacher is one who brings his or her learners up to his or her level in terms of knowledge. But in practice this is not possible and a teacher can only raise the mean of a class up to some extent depending on the capability of the class. In the entire population, the best solution is considered as the teacher (X_{teacher}). In the teacher phase the teacher tries to enhance the results of other individuals (X_i) by increasing the mean result of the classroom (X_{mean}) towards his/her position (X_{teacher}). In order to maintain stochastic features of the search, two randomly-generated Parameters r and TF are applied in update formula for the solution Xi as:

$$X_{New} = X_i + r (X_{Teacher} - TF * X_{Mean})$$

Where r is the random number considered between the range of 0 and 1 and

TF = Teaching factor which is considered as 1 or 2:

$$TF_i = \text{round} [1 + \text{rand} (0, 1) \{2-1\}]$$

Moreover, X_{new} and X_i are the new and existing solution of i.

Mean of population is calculated

$$\text{Mean} (X_{Mean}) = \text{Total make span} / \text{Total no of sequences}$$

$$= 3699/34 = 145.2 \approx 145$$

$$= 11-14-8-1-5-2-12-6-9-15-13-10-16-3-7-17-4$$

The best solution will act as a teacher for that iteration

$$X_{teacher} = X_f (X) = \text{min.}$$

$$X_{teacher} = 8-14-5-11-1-9-12-6-15-2-10-16-3-7-13-4-17$$

The difference between the X_{Teacher} and X_{Mean} is expressed as Difference, D = r (X_{Teacher} - TF * X_{Mean}).

$$= 0.85 \{ (8-14-5-11-1-9-12-6-15-2-10-16-3-7-13-4-17) - 2 * (11-14-8-1-5-2-12-6-9-15-13-10-16-3-7-17-4) \}$$

Subtracting the two vectors X_{Teacher} and X_{Mean} (absolute value is taken) and multiplying it with random number 0.85 and rounding off, we get

$$\text{Difference, } D = 0.85 \{ (8-14-5-11-1-9-12-6-15-2-10-16-3-7-13-4-17) - (22-28-16-2-10-4-24-12-18-30-26-20-32-6-14-34-8) \}$$

$$\text{Difference, } D = 0.85(14-14-11-9-9-5-12-6-3-28-16-4-29-1-1-30-9)$$

$$\text{Difference, } D = (11.9-11.9-9.35-7.65-7.65-4.25-10.2-5.1-2.55-23.8-13.6-3.4-24.65-0.85-0.85-25.5-7.65)$$

$$\text{Difference, } D = (12-12-9-8-8-4-10-5-3-24-14-3-25-1-1-25-8)$$

The T_F value is considered as one or two. The difference obtained is added to the current solution to update its values using

$$X_{new, D} = X_{old, D} + \text{Difference, } D$$

$$\text{For example } 1^{st} \text{ sequence as } X_{old, D} \text{ is considered}$$

$$= (8-14-5-11-1-9-12-6-15-2-10-16-3-7-13-4-17) + (12-12-9-8-8-4-10-5-3-24-14-3-25-1-1-25-8)$$

$$X_{new, D} = 20-26-14-19-9-13-22-11-18-26-24-19-28-8-14-29-25$$

Convert the values above 17 to allow max value within the bounds.

$$X_{new, D} = 3-9-14-2-9-13-5-11-1-9-7-2-11-8-14-12-8$$

In the above sequence few operations are missing and some are repeated to handle this a corrected repair function is used. Thus the resulting sequence after repair is

$$X_{new, D} = 3-9-14-2-10-13-5-11-1-4-7-17-16-8-15-12-6$$

The above sequence is repaired by using a repair function, in order to avoid repetitions and to follow precedence norms. The resulting sequence after repair is shown below.

$$X_{new} = 1-8-14-2-9-11-5-12-3-4-6-15-16-10-17-13-7$$

If the new sequence makespan value (after teacher phase) is less than that of the original sequence, then the new one is stored in place of the original one. In case if the algorithm was not able to find a better solution the original sequence remains the same.

Step 5: Learner Phase

Throughout this phase, the student X_i interacts randomly with another student X_j (i ≠ j) in order to improve his/her knowledge. In the case that X_j is better than X_i i.e. f(X_j) < f(X_i) for minimization problem, X_i is moved towards X_j.

Otherwise it is moved away from X_j:

$$X_{new} = X_i + r. (X_j - X_i) \text{ if } f(X_i) > f(X_j) \quad (10)$$

$$X_{new} = X_i + r. (X_i - X_j) \text{ if } f(X_i) < f(X_j) \quad (11)$$

Two learners (5th and 10th sequences) are randomly selected from the population (Table II) as an example.

$$(5-14-11-8-1-12-6-9-15-2-16-13-10-3-7-4-17) \text{ and } (14-8-5-11-1-9-15-12-2-6-7-10-3-16-13-17-4)$$

If f (5th makespan) < f (10th makespan) use 3rd equation

$$X_{new, i} = X_{old, i} + r_i (X_i - X_j)$$

$$X_{new, i} = (1-8-14-2-9-11-5-12-3-4-6-15-16-10-17-13-7) + 0.85 \{ (5-14-11-8-1-12-6-9-15-2-16-13-10-3-7-4-17) - (14-8-5-11-1-9-15-12-2-6-7-10-3-16-13-17-4) \}$$

$$X_{new, i} = (1-8-14-2-9-11-5-12-3-4-6-15-16-10-17-13-7) + 0.85 (9-6-6-3-0-3-9-3-13-4-9-3-7-13-6-13-13)$$

$$X_{new, i} = (1-8-14-2-9-11-5-12-3-4-6-15-16-10-17-13-7) + (8-5-5-3-0-3-8-3-11-3-8-3-6-11-5-11-11)$$

$$X_{new, i} = 9-13-19-5-9-14-13-15-14-7-14-18-22-21-22-24-18$$

Convert the values above 17 to allow max value within the bounds.

$$X_{new,i} = 9- 13- 2- 5- 9- 14- 13- 15- 14- 7- 14- 1- 5- 4- 5- 7- 1$$

In the above sequence few operations are missing and few are repeated. Hence it is repaired using the corrected repair function. The resulting sequence after repair is

$$X_{new,i} = 9- 13- 2- 5- 10- 14- 11- 15- 16- 7- 17- 1- 6- 4- 12- 8- 3$$

This sequence is corrected by the repair function for precedence requirements and the output is

$$X_{new,i} = 8- 11- 1- 5- 9- 14- 12- 15- 16- 6- 17- 2- 7- 3- 13- 10- 4$$

If the makespan value of the new sequence (after learner phase) is less than the old sequence, the new sequence is stored in place of the old sequence. In case where the algorithm could not find a better sequence after learner phase, then it stores the original sequence (generated sequence).

Step 6: The above procedure has been applied for all 34 sequences and minimum make span values are found after 20 runs.

Step 7: After getting the final sequence from each iteration crossover and mutation concepts are utilized which were hired from sheep flock heredity algorithm as explained in detail in article IV section B

Step 8: Receptor editing:

The editing of the chromosomes in the population after the cross over operation is known as receptor editing. In this process a number of worst makespan value chromosomes are eliminated from the population and randomly generated chromosomes are added in those places. After editing the chromosomes in the population the new population has gone to next iteration until termination criterion is reached.

Step 9: Termination criterion:

The crossover, selection, mutation and receptor editing are repeated till the termination criterion is satisfied.

In the present work repeating the procedure for number of generations is taken as the termination criterion.

Step 10: The evaluated values of different parameters in arriving at the makespan after 1000 iterations for the best sequence is presented in Table III.

Table III shows scheduling of operations through hybrid teaching learning-based optimization algorithm for job set 9 layout 1. The operational completion time (makespan) is 116 minutes.

Table-I: data related jobset 9

Job set : 9				
Layout: 1		No of Jobs: 5		No of operations: 17
Job 1	Job 2	Job 3	Job 4	Job 5
M3-M1-M2-M4	M3-M2-M4	M1-M2-M4	M2-M3-M4	M3-M1-M2-M4
1 - 2 - 3 - 4	5 - 6 - 7	8 - 9 - 10	11 - 12 - 13	14- 15- 16- 17

Table –II : Generated population size for the HTLBO

S.No	Sequence	Makespan
1	8-14-5-11-1-9-12-6-15-2-10-16-3-7-13-4-17	128
2	1-11-8-5-14-9-2-12-15-6-16-10-7-13-3-17-4	132
3	14-8-1-11-5-9-15-2-6-12-16-13-3-10-7-4-17	136
4	1-14-8-5-11-15-2-12-9-6-10-16-3-13-7-17-4	137
5	5-14-11-8-1-12-6-9-15-2-16-13-10-3-7-4-17	138
6	8-5-14-1-11-6-2-15-12-9-7-3-16-10-13-17-4	138
7	8-14-1-11-5-12-2-15-9-6-16-7-13-10-3-17-4	139
8	14-11-1-8-5-2-9-12-6-15-10-7-13-16-3-17-4	140
9	5-1-11-14-8-6-12-9-2-15-3-10-16-7-13-4-17	141
10	14-8-5-11-1-9-15-12-2-6-7-10-3-16-13-17-4	141
11	5-1-14-11-8-12-6-2-9-15-10-7-3-13-16-4-17	142
12	14-5-1-11-8-6-15-12-9-2-3-7-16-13-10-17-4	142
13	5-11-14-1-8-15-2-12-6-9-16-7-13-3-10-4-17	142
14	11-14-8-5-1-2-6-12-9-15-7-10-16-3-13-4-17	142
15	8-1-11-14-5-6-2-12-15-9-7-3-13-16-10-17-4	143
16	5-14-8-1-11-6-15-9-2-12-3-10-16-13-7-4-17	143
17	14-8-11-1-5-6-2-9-15-12-7-10-16-13-3-17-4	144
18	11-14-8-1-5-2-12-6-9-15-13-10-16-3-7-17-4	145
19	1-14-5-8-11-12-6-9-15-2-16-13-10-3-7-4-17	147
20	11-8-5-1-14-6-9-15-2-12-7-16-13-3-10-4-17	147
21	1-8-5-14-11-12-9-15-6-2-10-3-13-7-16-4-17	148
22	14-11-1-5-8-2-9-6-15-12-7-10-16-13-3-17-4	148



23	11-14-5-8-1-9-12-2-15-6-13-7-3-16-10-17-4	148
24	1-8-5-11-14-9-12-6-2-15-13-10-7-16-3-4-17	149
25	1-11-8-5-14-9-15-6-2-12-16-13-3-7-10-17-4	150
26	8-1-14-5-11-9-15-12-6-2-7-10-3-13-16-4-17	150
27	8-11-5-1-14-2-12-6-15-9-7-10-13-3-16-4-17	151
28	8-1-11-5-14-12-9-2-15-6-7-10-3-13-16-17-4	152
29	8-11-1-14-5-12-2-6-15-9-10-16-3-13-7-17-4	152
30	8-1-5-11-14-15-2-6-9-12-13-3-7-16-10-17-4	154
31	5-8-11-1-14-15-2-6-9-12-13-7-10-16-3-17-4	154
32	1-11-5-14-8-15-2-6-9-12-3-10-16-13-7-4-17	156
33	14-1-5-11-8-15-12-2-9-6-13-10-7-3-16-17-4	158
34	8-1-5-14-11-12-6-2-9-15-10-7-13-3-16-17-4	163

Table-III: Schedule Of Operations Through Htlbo (Problem Set 9 And Layout 1)

Operation Number	Machine Number	Vehicle Number	Travel Time	Job Reach	Job Ready	Make Span
5	3	1	0	10	10	26
11	2	2	0	8	8	28
14	3	1	18	28	28	42
8	1	2	18	24	24	45
1	3	1	36	46	46	55
6	2	2	32	38	38	49
12	3	2	38	44	55	77
15	1	2	44	52	52	68
9	2	2	52	58	58	76
2	1	1	55	63	68	80
7	4	2	58	66	66	75
16	2	1	68	74	76	89
13	4	2	77	83	83	94
3	2	1	80	86	89	98
10	4	1	86	94	94	101
17	4	2	91	99	101	110
4	4	1	102	110	110	116

V. RESULT AND DISCUSSION

The results obtained using the proposed Hybrid Teaching Learning based Optimization (HTLBO) for the 82 problems, that is 40 problems done with $t/p > 0.25$ and also 42 problems done with $t/p < 0.25$ are presented in the below Tables IV and V. Comparisons of these results with the results obtained by using priority rules proposed by (FCFS, SPT, LPT, Nageswararao et al. 2017) and results obtained using

heuristics proposed by (NEH, Prakash babu et al, 2018, FUZZY, P. B. Kanakavalli et al, 2018) is also done and tabulated in Table IV and V. A code is used to designate the example problems which are given in the first column. The digits that follow 1.1 indicate the job set and the layout. In t/p ratio < 0.25 table another digit is appended to the code. Here-having a 0 or 1 as the last digit implies that the process times are doubled or tripled- respectively- where in both cases travel times are halved.

Table-IV: Comparison of makespan values (for $t/p > 0.25$)

Job. No	t/p	FCFS	SPT	LPT	NEH	FUZZY	HTLBO
1.1	0.59	173	193	177	165	208	96
2.1	0.61	158	158	177	169	170	113
3.1	0.59	202	224	198	195	211	120
4.1	0.91	263	267	264	260	268	116
5.1	0.85	148	164	148	147	174	89
6.1	0.78	231	240	227	225	233	132
7.1	0.78	195	210	201	173	196	132
8.1	0.58	261	261	266	261	261	185

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9.1	0.61	270	277	268	259	273	116
10.1	0.55	308	308	310	305	315	167
1.2	0.47	143	173	165	147	188	82
2.2	0.49	124	124	130	116	127	86
3.2	0.47	162	188	160	154	178	96
4.2	0.73	217	223	224	215	232	90
5.2	0.68	118	144	131	117	156	73
6.2	0.54	180	169	165	158	175	108
7.2	0.62	149	160	149	136	139	91
8.2	0.46	181	181	198	181	181	159
9.2	0.49	250	249	244	205	249	104
10.2	0.44	290	288	287	274	274	148
1.3	0.52	145	175	167	145	190	84
2.3	0.54	130	130	136	122	133	100
3.3	0.51	160	190	162	158	176	102
4.3	0.8	233	237	230	226	234	96
5.3	0.74	120	146	133	117	156	76
6.3	0.54	182	171	167	160	177	116
7.3	0.68	155	166	151	138	141	104
8.3	0.5	183	183	200	183	183	169
9.3	0.53	252	251	246	207	251	106
10.3	0.49	293	294	293	280	280	154
1.4	0.74	189	207	189	189	228	104
2.4	0.77	174	174	174	169	190	124
3.4	0.74	220	250	212	213	225	130
4.4	1.14	301	301	298	298	294	128
5.4	1.06	171	189	171	171	193	97
6.4	0.78	249	252	237	234	243	140
7.4	0.97	217	242	151	192	232	154
8.4	0.72	285	285	200	285	285	195
9.4	0.76	292	311	290	285	295	123
10.4	0.69	350	350	345	345	353	178

Table – V: Comparison of makespan values (for $t/p < 0.25$)

Job.No	t/p	FCFS	SPT	LPT	NEH	FUZZY	HTLBO
1.10	0.15	207	248	252	207	278	126
2.10	0.15	217	217	225	185	208	148
3.10	0.15	257	327	282	255	300	162
4.10	0.15	303	328	317	277	352	123
5.10	0.21	152	190	187	154	225	102
6.10	0.16	304	281	297	272	294	192
7.10	0.19	231	240	264	213	235	137
8.10	0.14	338	338	347	332	338	292
9.10	0.15	390	367	359	324	382	182
10.10	0.14	452	429	444	398	393	262
1.20	0.12	194	238	246	197	268	123
2.20	0.12	194	194	206	167	187	143
3.20	0.12	241	311	270	241	285	159
4.20	0.12	285	312	298	248	340	116
5.20	0.17	142	180	184	143	217	100
6.20	0.12	292	260	284	251	277	187
7.20	0.15	212	218	249	188	210	136
8.20	0.11	306	319	334	306	306	287
9.20	0.12	380	355	347	309	372	179
10.20	0.11	445	423	439	388	384	259
1.30	0.13	195	239	247	196	169	122
2.30	0.13	197	197	209	170	190	146
3.30	0.13	240	312	271	240	284	160
4.30	0.13	292	317	301	255	339	117
5.30	0.18	141	181	183	143	216	99

6.30	0.24	296	261	285	252	278	188
7.30	0.17	215	221	250	191	213	137
8.30	0.13	307	320	335	307	307	288
9.30	0.13	381	356	348	310	373	180
10.30	0.12	448	426	442	391	387	260
1.40	0.18	213	255	254	213	288	124
2.41	0.13	307	307	319	267	293	217
3.40	0.18	261	330	282	258	305	162
3.41	0.12	370	476	411	310	435	239
4.41	0.19	434	471	451	393	504	177
5.41	0.18	218	269	270	222	321	148
6.40	0.19	310	288	299	275	303	189
7.40	0.24	239	251	270	221	246	138
7.41	0.16	329	344	385	224	332	203
8.40	0.18	343	343	349	339	343	293
9.40	0.19	396	379	370	325	388	182
10.40	0.17	466	445	455	415	408	265

Computations of completion times (makespans) for different combinations of job sets and layouts for Hybrid Teaching Learning Based Optimization algorithm, Priority rules (FCFS, SPT, LPT, Nageswara rao et al. 2017), Heuristic (NEH, Prakash babu et al, 2018, FUZZY, P. B. Kanakavalli et al, 2018) with $t/p > 0.25$ are done and tabulated in Table IV. From Table IV it can be observed that, out of 40 problems, 40 problems gives better results using HTLBO when compared with all other five algorithms (100%). Computations of completion time for different combinations of job sets and layouts for Hybrid Teaching Learning Based Optimization algorithm, Priority

rules (FCFS, SPT, LPT, Nageswara rao et al. 2017), Heuristic (NEH, Prakash babu et al, 2018, FUZZY, P. B. Kanakavalli et al, 2018) with $t/p < 0.25$ are done and tabulated in Table V. From Table V it can be observed that out of 42 problems, 42 problems give better results using HTLBO when compared with all other five algorithms (100%).

VI. CONCLUSION

Flexible Manufacturing system is considered as better option to face the challenges of global competition. But for successful implementation efficient scheduling is essential. Scheduling of an FMS is a very difficult problem because of other consideration like material handling. In this work an attempt has been made to solve the problem of scheduling both the machines and AGVs simultaneously by hybrid metaheuristic algorithm the following conclusions are drawn from this work. Performances of Hybrid Metaheuristic Algorithm is evaluated by considering 82 benchmark problems consisting of different job sets and layout configurations. From the comparison of these results Hybrid Teaching Learning Based Optimization algorithm (HTLBO) yielded improved results in 82 problems.

VII. SCOPE OF FUTURE WORK

In this research work simulating metaheuristic Algorithms to solve simultaneous scheduling problems in FMS. There is scope for further research work in the following aspects: In FMS jobs are entered with different priorities and the problem can be made dynamic in nature.

When required sequence needs to reschedule. The simultaneous scheduling problem can be extended further by including AS/RS system. Real time issues like traffic jamming- without buffer space- machine breakdown can also be considered.

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