Abstract — Impulse noise in images culminates to the loss of valuable information. This paper proposes an efficient fuzzy filter for suppression of impulse noise in images (EFFSIN). Firstly, impulse noise is effectively detected by the proposed algorithm with the utilization of Fuzzy C-Means (FCM) in two stages. Only legitimate pixels are restored after fair distinction of noisy pixel from edge pixel. Proper restoration of noisy pixel following effective detection by proposed work leads to low miss detection (MD) and false alarm (FA) rates. Simulation results depict the efficacy of the proposed filter with reference to peak signal-to-noise ratio (PSNR) and structural similarity index measure (SSIM).

Index Terms — Impulse noise, Fuzzy filter, Noise suppression, Peak signal to noise ratio

I. INTRODUCTION

Impulse noise often degrades the images and ruin the valuable information present in an image. The quality of digital images is demolished by impulse noise at the time of procurement of images and their transposal. Faulty memory locations or impaired pixel sensors can result in images corrupted with impulse noise. Images acquired by low resolution digital cameras, scanned images and satellite images need to be processed before further use. Transmitted television signals are often affected by impulse noise and require processing. Impulse noise can either mark up the intensity values or mark the levels low, which can cause serious depletion in the quality of image. Thus noise removal is one of the most critical pre-processing operation, an image should undergo before further image analysis.

In literature, a variety of methods are present for removing impulse noise, broadly classified as linear and non-linear. Impulse noise is not adequately eliminated by linear filters as they tend to obscure the edges of an image. Then again, non-linear filters are more qualified for managing impulse noise because of their improved execution as for edge protection and noise suppression. Various traditional non-linear filters with fuzzy reasoning have risen in the previous couple of years. The application of fuzzy reasoning for the detection and impulse noise restoration is considered vital. Initially Bezdek and Castelaz [1] studied the fuzzy classifier for feature selection. The fuzzy set approach for the enhancement of images was introduced by Pal and King [2]. They developed an algorithm for the progressive use of fuzzy operator [3].

Over the years, fuzzy based algorithms have shown various variations in their approach of working. Fuzzy mean filters are productive in their nature in terms of impulse noise removal [4–6]. Fuzzy logic used in conjunction with the standard median filter have resulted in various efficient and more robust techniques as compared to fuzzy mean filters for impulse noise removal and detection [7–12].

Histogram of an image acts as an efficient tool for retrieving information. Histogram based fuzzy algorithms are also present in literature which works well for the assessment of impulse noise in images. J.H Wang et.al. suggested an algorithm developed by using a set of fuzzy membership functions with the initial parameters based on histogram of input image [13]. S. Schulte et.al. utilized the image histogram to find out impulse noise in color images [14]. In addition with the histogram, fuzzy K-means clustering along with fuzzy-support vector machine (FSVM) classifier is used in [15]. Many histogram-based fuzzy filters and fuzzy median filters perform effectively in terms of detection of impulse noise but proper restoration of noisy pixel is not achieved. It results in high false alarm (FA) rates. Edges present in an image are often detected as impulse noise which gives rise to greater miss detection (MD) rates.

In the recent years, various neuro-fuzzy filters along with evolutionary algorithms have evolved to deal with impulse noise and edge detection such as techniques based on Particle swarm optimization (PSO) [16,17], ant colony optimization [18] and bacterial foraging [19,20] by Verma et.al. Neuro-fuzzy filter with optimized intelligent water drop technique presented by Devi and Soranamageswari in [21] and many more. Neuro-fuzzy filters provide fair results but are complex in nature with increased computational time and cost.

Various algorithms are present in literature which are based on fuzzy logic in combination with other state-of-art filters to handle impulse noise. Each method has its own benefits and restrictions, but fuzzy clustering shows supremacy over other techniques due to its simple structure, less computation time and robust performance even in high noisy environment. Fuzzy C-Means (FCM) is among the popular sought algorithm utilized for grouping of information [22]. FCM is integrated for impulse noise detection by Singh and Verma in [23] which results in low miss detection rates and high PSNR values but false alarm rates are not decreased. After proper detection of noise, its subsequent restoration is important to get a high quality image. The proposed work also focuses on the efficient restoration of noisy pixel tampered with impulse noise.
II. PROPOSED WORK

The basic characteristics of an image are impaired with the intrusion of impulse noise. Impulse noise is alias as Salt and pepper noise in literature. The original pixel values are altered by the extreme intensity values of the dynamic range usually 0 or 255. The proposed work is dynamic in nature which significantly removes impulse noise from images without compromising on the existing edge details. Even if the pixels are detected as noisy, algorithm performs restoration after checking whether the identified noisy pixel is impulse noise or an edge value whose true value is 0 or 255. This mechanism results in a potent algorithm with lower false alarm (FA) and miss detection (MD) values.

Fuzzy C-Means (FCM) is a widely recognized procedure for data clustering. This technique was introduced by Dunn[24] and Bezdek[25] further enhanced it. Since its invention, it is extensively used in various fields to classify data. It provides excellent results for overlapped data sets. FCM is employed in the detection phase twice for the grouping of pixels among three major categories i.e. pepper noise, noise-free and salt noise.

A. Impulse Noise Detection

The proposed algorithm performs impulse noise detection in two phases. The initial phase attempts to detect noise on global basis therefore a bigger window size of 21×21 is used to extract relevant information from a noisy image.

Phase I

1. Center a 21×21 size window on every image pixel.
2. Pixel under inspection is referred as v(l, f) i.e value at ith location and jth location in spatial domain.
3. FCM classify the adjacent 441 pixels unsupervisely into three clusters.
4. Compute the the highest intensity value of pixel in each cluster respectively, denoted as H1, H2 and H3 such that H3 > H2 > H1.
5. Cluster with the highest intensity value as H1 is labelled as “pepper noise”, the group with H2 as its highest value is termed as “noise-free” and H3 belongs to “salt-noise” group. The following equation is used to evaluate that the pixel is affected with impulse noise or not.

\[
\begin{align*}
\text{pepper noise:} & \quad v(l', f') \leq H_1 \\
\text{noise free:} & \quad H_1 < v(l', f') \leq H_2 \\
\text{salt noise:} & \quad H_2 < v(l', f') \leq H_3
\end{align*}
\]

6. In case the pixel belongs to the “noise-free” group, it is not processed further and its original intensity value is retained, otherwise pixel is evaluated again in the second phase of detection.

Phase II

1. For the analysis of the noisy pixel on local basis, window size is altered to 7×7.
2. FCM classify the adjacent 49 pixels unsupervisely into three clusters.
3. Reiterate the steps 4) and 5) in the similar manner.
4. If v(l, f) falls into “noise-free” group, it is considered as an uncorrupted pixel and no transition is made in its original value, otherwise the noisy pixel is restored.

B. Impulse Noise Restoration

An image is comprised of many fine details and sometimes the true value of a pixel or edge values are identified as noise. To minimize the false alarm and miss detection rates, it is important to differentiate between an edge pixel and noisy pixel. The double-phase analysis of a pixel by the proposed algorithm helps to identify the noise affected pixels in a more robust way. The proposed work also focuses on proper restoration of noisy pixels such that edges are preserved and an high quality image is perceived at the user end. For proper classification of noisy pixels from edge pixels, the following steps are performed at the restoration stage:

1. For a noisy pixel, consider the clusters generated by FCM with 7×7 window, having the highest intensity value of H1 and H2 respectively.
2. In each cluster, count the number of 0 and 255 respectively and its value is stored in a function denoted by “COUNT1” for number of 0 incase of “pepper-noise” and “COUNT2” for number of 255 incase of “salt-noise”.
3. If COUNT1 ≤ 2 or COUNT2 ≤ 2 then the pixel under evaluation is considered as noisy and will be restored.
4. If COUNT1 ≥ 3 or COUNT2 ≥ 3 then take a 3×3 window placed on processing pixel to check if its a noisy pixel or an edge.
5. The following two cases are considered for image restoration by taking the eight adjacent pixels of the center pixel i.e. N8 into account:

   Case I: If N8 has all 0 or 255 then do not perform any restoration as it can be an edge value.

   Case II: If N8 has 0 or 255 greater than one then expand window size to 5×5 to check for any possible edge.

\[
\begin{array}{cccccc}
  v^{24} & v^{10} & v^{11} & v^{12} \\
  v^{23} & v^{10} & v^{11} & v^{12} \\
  v^{22} & v^{10} & v^{11} & v^{12} \\
  v^{21} & v^{10} & v^{11} & v^{12} \\
  v^{20} & v^{19} & v^{18} & v^{17} & v^{16} \\
\end{array}
\]

Let the pixel under processing is “NOISY” as shown in fig 1. The adjacent pixels are denoted as v0 to v24.

The following rules are utilized to cross-check whether the pixel needs to be restored or not.

Rule 1:

IF (v0 is NOISY) AND (v2 and v12 are NOISY) AND (v6 and v20 are NOISY) THEN (v0 is EDGE)
Rule 2:  
\[
\text{IF} \ (\nu^1 \text{ is NOISY}) \ \text{AND} \ (\nu^1 \text{ and } \nu^{10} \text{ are NOISY}) \ \text{AND} \ (\nu^1 \text{ and } \nu^{16} \text{ are NOISY}) \ \text{THEN} \ (\nu^1 \text{ is EDGE})
\]

Rule 3:  
\[
\text{IF} \ (\nu^0 \text{ is NOISY}) \ \text{AND} \ (\nu^8 \text{ and } \nu^{14} \text{ are NOISY}) \ \text{AND} \ (\nu^3 \text{ and } \nu^{14} \text{ are NOISY}) \ \text{THEN} \ (\nu^0 \text{ is EDGE})
\]

Rule 4:  
\[
\text{IF} \ (\nu^0 \text{ is NOISY}) \ \text{AND} \ (\nu^8 \text{ and } \nu^{22} \text{ are NOISY}) \ \text{AND} \ (\nu^3 \text{ and } \nu^{v4} \text{ are NOISY}) \ \text{THEN} \ (\nu^0 \text{ is EDGE})
\]

“NOISY” indicates the pixel value as 0 or 255. Noisy Pixel value should be either 0 in all cases or 255 during the complete analysis of pixel with above mentioned rules. Edges indicate the significant regional transitions of intensity values in an image. Constant occurrence of noisy pixels with same intensity value of either 0 or 255 imply the presence of a possible edge.

Pixel evaluated as “NOISY” via any of the rules stated in the preceding step is replaced with the median value of the 5x5 window and pixel evaluated as “EDGE” is not modified. The separation of noisy pixels from possible edge pixels lowers the False Alarm rates and Miss detection rates by the proposed algorithm. It also increases the PSNR and SSIM values. The standard median filter[26] is a well known powerful filter in the area of image processing and is used for various applications including impulse noise removal. If used directly it can lead to loss of fine details/edges present in an image. The proposed work presents a sturdy technique which uses the median filter after the analysis of impulse noise in an image which enhances its performance.

**figure 2**: Block Diagram of the Proposed Scheme

**C. Exemplification of Proposed filter**

An exemplification of the proposed work is presented for a more clear perception.

**figure 3**: 7x7 window

A 7x7 window is used for demonstration of work instead of 21 x21 window for the first impulse noise detection phase for a crisp view. FCM classify the adjacent 49 pixels unsupervisely in three clusters let Q,R and S.

\[
\begin{align*}
Q&=[193,201,201,210,211,215,236,250,255,255,255]\,\text{salt noise if } \nu l l=0\,\text{and } \nu l l\text{ free if } \nu l l=165, \text{and } \nu l l=255 \text{in equation (1).}
\end{align*}
\]

The highest value from each cluster is calculated and labeled as \(H_1, H_2 \text{ and } H_3\) such that \(H_i < H_j < H_k\). Substitute the values of \(H_1=63, H_2=165\) and \(H_3=255\) in equation (1).

\[
\begin{align*}
S&=[0,0,0,0,0,0,0,10,13,16,20,23,30,32,36,42,46,47,50,52,53,63,63] \\
\text{It is depicted from the above equation that the pixel under processing is “pepper-noise”. Similarly, this pixel is again examined in the second detection phase with window size of 7x7, for the presence of impulse noise. Likewise it is discovered as a noisy pixel in second detection phase. For impulse noise restoration, consider the clusters with highest value of } \(H_1=63\) \text{ and } \(H_2=255\). \text{ The pixel is marked as “pepper-noise”therefore “COUNT1” is computed. COUNT1=9. In this case, COUNT1 ≥ 3, so 3x3 is centered on noisy pixel. According to step (5) case II of impulse noise restoration the window is expanded to 5x5.}
\end{align*}
\]

**figure 3**: Expansion of window size and final result

Analysis for any possible edge is performed using Rule 1, 2, 3 and 4. Rule 1 is true for present pixel therefore, it is marked as EDGE and no restoration is done.

**III. EXPERIMENTAL RESULTS**

The proposed work abbreviated as EFFSIN is simulated for impulse noise of varying densities as well as examined in contrast with other state-of-art filters present in literature. The similarity measures employed for the performance evaluation of our work are Peak signal-to-noise ratio (PSNR)[27, 28], structural similarity index (SSIM)[30], False alarm (FA) and Miss detection (MD) values[29].

PSNR (peak signal to noise ratio) is computed by:

\[
PSNR( f , I ) = 10\log \left( \frac{1}{MSE( f , I )} \right) 
\]

I stand for the original image sequence, f stand for the filtered image sequence of \( N \times M \) size. High value of PSNR indicates greater uniformity between noise-free image and restored image.

SSIM is calculated using the following equation:
Edge Preserving Fuzzy Filter for Suppression of Impulse Noise in Images

\[ SSIM = \frac{(2\mu_I\mu_f + c_1) + (2\sigma_I + c_2)}{(\mu_I^2 + \mu_f^2 + c_1) + (\sigma_I^2 + \sigma_f^2 + c_2)} \] (4)

Variables \( \alpha_1, \alpha_2 \) and \( \alpha_3 \) define the relative importance of the three components. When \( \alpha_1 = 1 \) and \( \alpha_2 = \alpha_3 \), SSIM is deduced as in equation (4).

Apart from PSNR and SSIM, the proposed algorithm has employed False alarm (FA) and miss detection (MD) rates as quality metrics. A difference based method[23] is used for the evaluation of FA and MD, which generates a noise chart on the basis of differences computed between noise chart and original image. Total correct detection, False alarm and Miss detection are shown in figure 4 where, ‘1’ in the noise chart indicates presence of noise, whereas ‘0’ imply noise free.

From figure 4, it is clear that False Alarm arises when a noise-free pixel is identified as noisy and marked as ‘1’ in the noise chart. Miss detection takes place when a noisy pixel is identified as noise-free and marked as ‘0’ in the noise chart.

The standard gray scale test image ‘lena’ 512 × 512 is used for analysis of our work with other filters. Table 1 represents the analysis of PSNR and SSIM values for varying filters for impulse noise and our work. Table 2 provides PSNR and SSIM values by EFFSIN for varying test images at 30% noise and there is illustration of FA and MD values in Table 3.

![Figure 4: Difference based method for FA and MD](image)

**Table 1: PSNR and SSIM results for “Lena”**

<table>
<thead>
<tr>
<th>Noise density %</th>
<th>Method</th>
<th>10</th>
<th>20</th>
<th>30</th>
<th>40</th>
<th>50</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>PSNR</td>
<td>SSIM</td>
<td>PSNR</td>
<td>SSIM</td>
<td>PSNR</td>
<td>SSIM</td>
</tr>
<tr>
<td>FSM[8]</td>
<td>36.07</td>
<td>0.9117</td>
<td>34.12</td>
<td>0.9001</td>
<td>32.39</td>
<td>0.8541</td>
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### Table 3: FA and MD values

<table>
<thead>
<tr>
<th>Noise%</th>
<th>FSBH</th>
<th>AFSM</th>
<th>HDIND</th>
<th>EFFSIN</th>
<th>FSBH</th>
<th>AFSM</th>
<th>HDIND</th>
<th>EFFSIN</th>
</tr>
</thead>
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<tr>
<td>10</td>
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<td>0</td>
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<td>0</td>
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<tr>
<td>30</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>2</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>50</td>
<td>23</td>
<td>6</td>
<td>0</td>
<td>0</td>
<td>7</td>
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<td>4</td>
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<td>70</td>
<td>31</td>
<td>14</td>
<td>2</td>
<td>1</td>
<td>12</td>
<td>11</td>
<td>7</td>
<td>3</td>
</tr>
<tr>
<td>90</td>
<td>36</td>
<td>21</td>
<td>2</td>
<td>2</td>
<td>19</td>
<td>15</td>
<td>9</td>
<td>4</td>
</tr>
</tbody>
</table>

### Table 2: PSNR and SSIM results for various images using EFFSIN

<table>
<thead>
<tr>
<th>Image name</th>
<th>PSNR</th>
<th>SSIM</th>
<th>PSNR</th>
<th>SSIM</th>
<th>PSNR</th>
<th>SSIM</th>
</tr>
</thead>
<tbody>
<tr>
<td>Living room</td>
<td>38.79</td>
<td>0.8992</td>
<td>37.68</td>
<td>0.8876</td>
<td>38.48</td>
<td>0.9007</td>
</tr>
<tr>
<td>Woman Blonde</td>
<td>40.19</td>
<td>0.9237</td>
<td>39.70</td>
<td>0.9192</td>
<td>37.34</td>
<td>0.8998</td>
</tr>
<tr>
<td>Mandril</td>
<td>35.87</td>
<td>0.8922</td>
<td>35.18</td>
<td>0.8910</td>
<td>34.47</td>
<td>0.8848</td>
</tr>
<tr>
<td>Pirate</td>
<td>39.96</td>
<td>0.9015</td>
<td>38.63</td>
<td>0.8993</td>
<td>38.48</td>
<td>0.9007</td>
</tr>
<tr>
<td>Cameraman</td>
<td>39.03</td>
<td>0.9067</td>
<td>37.81</td>
<td>0.8981</td>
<td>36.77</td>
<td>0.8837</td>
</tr>
</tbody>
</table>

### Table 3: FA and MD values

<table>
<thead>
<tr>
<th>Image name</th>
<th>FSBH</th>
<th>AFSM</th>
<th>HDIND</th>
<th>EFFSIN</th>
</tr>
</thead>
<tbody>
<tr>
<td>Miss detection(MD)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>False Alarm(FA)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
From the analysis of mathematical data in Table 1, Table 2, and Table 3, it is clear that EFFSIN significantly surpass the contemporary techniques available for impulse noise. There is notable improvement in the results of HDIND after the incorporation of edge detecting feature in the impulse restoration phase. The proposed filter confers consistent performance with varying amount of noise. The $FA$ and $MD$ values are reduced remarkably. HDCNN yields good $PSNR$ and $SSIM$ values but is complex in nature with high computation time. The proposed filter is elementary in nature with less computation time. WAF does not preserve the fine details of the image and provides low quantitative results. Similarly, FSBH and AFSM do not reduce the $FA$ and $MD$ values. The proposed work is edge preserving in nature which provides relatively low False alarm rates and miss detection rates thereby improving the $PSNR$ and $SSIM$ values. It also gives efficient results for different test images.

The application of median filter after the assessment of possible edges has enhanced the quality of work. The qualitative results for “lena” in “figure 5”, “livingroom” in “figure 6” and “Womenblonde” in “figure 7” display the high conduct of the proposed filter for differing levels of impulse noise. All the simulation results are derived using MATLAB.

IV. CONCLUSION

In this paper, an edge preserving algorithm for the suppression of impulse noise is introduced. The two phase impulse noise detection and proper impulse noise restoration with the evaluation of possible edges makes it a coherent technique for impulse noise suppression. The extensive simulation results predict that the proposed work makes remarkable reduction in the False alarm rates.
it also excels quantitatively and qualitatively. An unequivocal approach of the proposed work enhances its performance with less computation time. The work can be extended further for impulse noise detection and restoration in color images and sequences.

REFERENCES


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Prof Om Prakash Verma holds a Ph.D degree (Electronics and communication engineering) awarded by Delhi University, Mtech(Communication and Radar Engineering) from (IIT) Indian Institute of Technology, Delhi and B.E from MNT,Jaipur.At present, He is Principal of GB Pant Govt. Engineering College,Delhi.Previously,He worked as HOD of Computer Science and engineering and Information Technology at Delhi Technological University,Delhi. His professional experience is over 25 years and has over 50 publications at international and national levels.For research, Image Processing, Soft Computing, Machine learning and Evolutionary Computing are his prime area of interest.He has conducted several research activities and has many awards and patents after his name.The valuable guidance of Prof Verma has helped to complete this work.

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