

Mathematical Modeling Development Of Medium Flow in Rotary-Pulse Device Channels

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Abstract: This paper considers the issues of mathematical modeling development of medium flow in rotary-pulse devices channels (RPD) which are used in the conditions of hydrodynamic cavitation for cleaning scale from technological lubricants.

Index Terms: Sludge deoiling, bottom sediments, laboratory installation, scientific research, automation, industrial enterprises

I. INTRODUCTION

A scientific search for progressive methods of treating fluids has shown that cavitation technologies, as well as devices implementing these technologies, can be one of the most effective methods. [1–6].

The basis of the oily sludge of bottom sediments is fine oily scale. Fine oily scale is laminal particles of different thickness, representing the ternary system “solid particles of iron oxides–water–technological lubricants”, which simultaneously have both hydrophilic (scale–water) and hydrophobic properties (oil–water), which makes it difficult to clean from oils.

In the conditions of hydrodynamic cavitation, the following model of descaling of process lubricants is proposed (Figure 1).

Oiled scale particles, falling into the cavitation cluster formed in the stator channel of the RPD, are under the influence of collapsing cavitation bubbles. Oil films that contaminate the surface of the scale are destroyed due to

spherical shock waves arising from the collapse of many cavitation bubbles removed from the surface being cleaned or from each other, as well as from the cumulative jets arising from the asymmetric collapse of bubbles that are near the surface being cleaned.

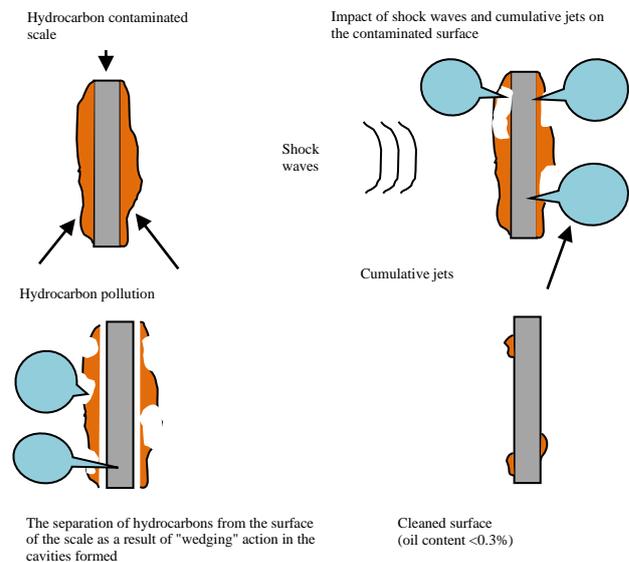


Figure 1 - Model of cleaning scale from technological lubricants under conditions of hydrodynamic cavitation

Due to the radial imbalance of forces on the surface of the cavitation bubble, the cumulative jet is directed toward the nearest surface. Its high-energy point impact on pollution leads to intensive destruction of the nearest surface. The cleaning effect in this case is comparable to the effects of countless brushes. Depending on the ratio of adhesion forces and cohesion, the gradual destruction of the pollution or its separation from the surface is possible

II. MATERIALS AND METHODS

Mathematical modeling development of medium flow in rotary-pulse devices channels (RPD)

In order to determine the energy consumption in the process of destruction of pollution on the surface of the slurry particle, we can use the following dependence:

$$\varepsilon = \frac{\eta \cdot E}{m_{DS}}, \quad (1)$$



Manuscript published on 30 April 2019.

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where ε – specific energy of destruction, J/kg;
 E – energy reported to destroy pollution from the outside, J;
 η – Efficiency, fractional;
 m_{ds} – mass of the destroyed surface, kg.
 In this case, the energy imparted by the contaminated sludge particle should be understood as the total energy created by cumulative microjet:

$$E = n \cdot E_{CM}, \quad (2)$$

where n – number of bubbles, pcs;
 E_{MC} – energy of a cumulative microjet, J.

If the energy of the cumulative microjet is forced to destructible pollution due to the impact, we obtain:

$$E_{CM} = \frac{m_{CM} \cdot v_{CM}^2}{2}, \quad (3)$$

where n – mass of cumulative microjet, kg;
 m_{CM} – cumulative microjet speed, m/s.

The mass of the cumulative microjet is determined from the expression:

$$m_{CM} = \rho_L \cdot V_{CM}, \quad (4)$$

where ρ_L – liquid density, kg/m³;
 V_{CM} – volume of cumulative microjet liquid, m³.

Considering the shape of a cumulative microjet cylindrical, its volume is equal to:

$$V_{CM} = l_{CM} \frac{\pi \cdot d_{CM}^2}{4}, \quad (5)$$

where l_{CM} – length of the cumulative microjet, m;
 d_{CM} – diameter of the cumulative microjet, m.

The diameter and length of the cumulative microjet [6] are determined by the following relations:

$$d_{CM} = 0,092 \cdot R_{MAX}; \quad l_{CM} = 0,116 \cdot R_{MAX}, \quad (6)$$

where R_{max} – maximum radius of the cavitation bubble (at the moment of collapse), m.

The speed of the cumulative jet [6] is determined by the expression:

$$v_{CM} = k \cdot v_c, \quad (7)$$

where v_c – cavitation bubble collapse rate, m/s;
 k – energy ratio ($k \approx 4$).

The collapse of the cavitation bubble rate [6] is determined by the dependence:

$$v_c = \sqrt{\frac{2}{3} \cdot \left(\left(\frac{R_{MAX}}{R_0} \right)^3 - 1 \right) \cdot \frac{P}{\rho_L}}, \quad (8)$$

where R_0 – the initial radius of the cavitation bubble (radius of the embryo), m;

P – pressure acting on the cavitation bubble, Pa.

The difficulty in the calculations is the determination of the initial and maximum radius of the cavitation bubble. From the works of I.M. Fedotkin [7, 8] it is known that the average radius of a cavitation bubble during hydrodynamic cavitation production is $R_{AR} = 20 \cdot 10^{-6}$. According to experimental data from the works of M.A. Promtov [6, 9] ratio is $R_{MAX}/R_0 = 3 \div 6$. Accept the ratio $R_{MAX}/R_0 = 4,5$.

Using dependencies (2)-(8), we can get an expression to determine the minimum value of the final radius of the cavitation bubble, at which the contamination of the slurry particle can be destroyed:

$$R_{MAX} = 4,5 \cdot \sqrt[3]{\frac{E}{33,8 \cdot n \cdot P}}. \quad (9)$$

Practical use of expression (9) allows to preliminarily estimate the energy required to destroy the contamination of the slurry particle (1), as well as to determine the number of cavitation bubbles and the magnitude of their pressure at which they collapse.

In this case, the energy released during the collapse of cavitation bubbles participates in the destruction of hydrocarbon compounds, i.e. breaks chemical bonds between atoms of molecules. This leads to the fact that the desorbed oil droplets pass into light fractions and are easily removed by subsequent classification.

III. RESULTS AND DISCUSSION

When calculating the RPD distinguish two tasks:

- calculation and design of a universal device designed for carrying out hydromechanical and heat exchange processes in liquid media;
- calculation and design of the device intended for a specific technological process.

Considering the first task, when a multifunctional apparatus is being designed, it is necessary to consider natural and relative criteria firstly and then economic criteria. Moreover, it is primarily necessary to operate with criteria that show technical and technological efficiency, and then minimize the cost of manufacturing the device.

Solving the second task, when the technological chain and the technological cycle are fully defined, it is necessary to make calculations using economic criteria, for example, the payback period of capital investments and net present value. Universal RPD are usually used in low-tonnage production with a wide range of products and for solving research problems. In large-scale industrial production, and when the use of a device for carrying out only one technological process is justified, the use of a specially designed RPD for this technological process is most effective. Universal RPD are designed in such a way that the main factors affecting the liquid heterogeneous processable medium are involved and give the greatest return.

The design and calculation methodology for RPD are discussed in detail in [10, 11]. According to their recommendations, a single-stage RPD was designed and manufactured.

The mathematical model that fully reflects the basic laws of non-stationary hydro-mechanical processes in an RPD chopper formed by a rotor channel and a stator and a radial gap between them (Figure 2) is the Bernoulli equation, recorded considering non-stationarity of the flow [12-15]:

$$\beta l \frac{dv}{dt} + \lambda l \frac{v^2}{2d} + \zeta \frac{v^2}{2} + \frac{Bv}{2d} = \frac{\Delta P}{\rho},$$



where β – coefficient of the amount of flow of the processed medium (for engineering calculations, it can be taken as equal to 1);

$v(t)$ – instantaneous value of the average over the channel cross-section velocity, m/s;

ρ – density of the processed medium, kg/m³;

l – modulator (breaker) length, m;

λ – hydraulic resistance coefficient;

d – diameter of rotor and stator channels, m;

ΔP – differential pressure on the modulator, Pa;

$\zeta(t)$ – total coefficient of local hydraulic resistance;

$B(t)$ – coefficient of hydraulic resistance, considering the pressure loss, depending on the flow rate;

ν – medium viscosity index, m²/s.

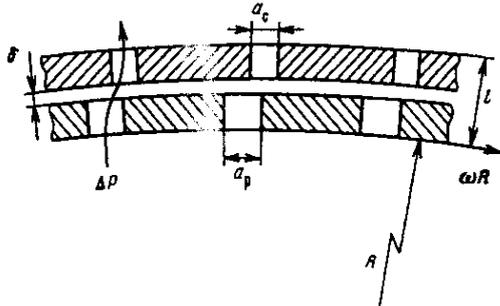


Figure 2 – The cross-section of the side walls of the RPD rotor and stator

Equation (1) differs from the usual Bernoulli equation in that the coefficients λ and ζ are “non-stationary”. They depend on time in accordance with changes in the velocity distribution, turbulent pulsations, and the average flow rate of the medium being processed [12, 16].

Consider that the pressure loss calculated taking into account the non-stationarity of the tangential voltage on the channel wall is only a few percent more than the pressure loss calculated for the stationary case, we take the coefficient λ equal to the stationary value. In studies of non-stationary hydro-mechanical processes in tubes [17] with local hydraulic resistance, it was found that using stationary values of the drag coefficient, the maximum error in calculating instantaneous averages over the cross section of flow velocities does not exceed 20%. That said, the function $\zeta(t)$ is taken to correspond to the stationary mode. It is assumed that this cannot significantly affect the nature of the function $v(t)$ [18, 19].

Thus, equation (10) takes the form:

$$l \frac{dv}{dt} + \frac{1}{2} \left(\lambda l \frac{v^2}{d} + \zeta(t)v^2 + B \frac{v\nu}{d} \right) = \frac{\Delta P}{\rho}. \quad (11)$$

Equation (11) is written considering comments on the coefficients β , λ and ζ .

The pressure generated by the outlet hole of the stator channel in the phase of positive pressure somewhat inhibits the movement of fluid.

Because the fact that the pressure source is a monopole-[13] radiating into space (solid angle $\Omega = 2\pi$), we can write:

$$\frac{dv(t-r/c)}{dt}; \quad P(t) = \rho \sqrt{\frac{S_0}{\pi}} \cdot \frac{dv}{dt}. \quad (12)$$

A similar effect is exerted by the pressure generated by the inlet of the rotor channel, since works in antiphase with an outlet. Then equation (11) takes the form:

$$\left[l + (1 + \Gamma) \sqrt{S_0/\pi} \right] \frac{dv}{dt} + \frac{1}{2} \left(\zeta(t)v^2 + B \frac{v\nu}{d} \right) = \frac{\Delta P}{\rho}, \quad (13)$$

where Γ – the ratio of the area of the stator channel outlet to the area of the rotor channel entrance, in our case $\Gamma=1$.

It can be seen from equation (13) that considering the effect of the generated variable pressure on the unsteady hydromechanical processes in the apparatus chopper reduces to increasing the effective length of the modulator to:

$$l_e = l + (1 + \Gamma) \sqrt{S_0/\pi}, \quad (14)$$

where S_0 – cross hole area of the stator channel, m².

It is also necessary to consider the pressure arising from the rotation of the medium in the rotor cavity and the centrifugal inertia forces acting:

$$\Delta P_{ci} = \rho \omega^2 R_r^2 / 2. \quad (15)$$

Then (13) is reduced to the form:

$$l_e \frac{dv}{dt} + \frac{1}{2} \left(\zeta(t)v^2 + \frac{Bv\nu}{d} \right) = \frac{\Delta P}{\rho} + \frac{\omega^2 R_r^2}{2}. \quad (16)$$

Analyzing this equation (16) without solving, it can be concluded that in the initial time interval, when the hydraulic resistance is large, and the speed of the processed medium is small, the dependence of speed on time is linear:

$$v(t) = \left(\frac{\Delta P}{\rho l_e} + \frac{\omega^2 R_r^2}{2 l_e} \right) t + v(0). \quad (17)$$

To bring equation (16) to the criterion dimensionless mind, the dimensional variables v and t must be replaced by the dimensionless variables w and τ using the relations

$$\begin{aligned} v &= v_0 w; \\ t &= t_0 \tau. \end{aligned} \quad (18)$$

Then equation (16) takes the form:

$$l_e \frac{dw}{dt} \cdot \frac{v_0}{t_0} + w^2 v_0^2 \left(\zeta(t) + v_0 w \frac{Bv}{2d} \right) = \frac{\Delta P}{\rho} + \frac{\omega^2 R_r^2}{2}. \quad (19)$$

Multiplying the terms of both sides of equation (19) by the value $t_0/l_e v_0$, we get

$$\frac{dw}{d\tau} + w^2 Ho_1 \zeta(\tau) + w \frac{B}{Re} = Ho_1 Eu + \frac{1}{Ho_2}. \quad (20)$$

The criteria included in equation (20) are as follows:

$$\begin{aligned} &\text{criterion of “longitudinal” homochronicity} \\ Ho_1 &= v_0 t_0 / 2 l_e; \end{aligned} \quad (21)$$

$$\begin{aligned} &\text{criterion of “transverse” homochronicity} \\ Ho_2 &= \omega^2 R_r^2 t_0 / 2 l_e v_0; \end{aligned} \quad (22)$$

$$\begin{aligned} &\text{Euler criterion} \\ Eu &= 2 \Delta P / \rho v_0^2; \end{aligned} \quad (23)$$



Reynolds criterion

$$Re = 2dl_e/vt_0. \tag{24}$$

The homochronic criterion characterizes the non-stationary nature of fluid flow in spaces bounded by solid walls, and Euler's criterion considers the effect of pressure drops on the process, representing the ratio of pressure forces and inertia forces. The scale of speed and time is chosen as follows (the rationale for the scale of speed and time is given below):

$$t_0 = a_s/\omega R_r; v_0 = \Delta Pt_0/\rho l_e, \tag{25}$$

where a_s – stator channel width, m;
 ω – rotor angular speed, s-1;
 R_r – rotor radius, m.

Considering (25) and the conversion of criteria (21)-(24), equation (20) takes the form:

$$\frac{dw}{d\tau} + w^2 Ho\zeta(\tau) + wB(\tau) \frac{Ho}{Re} = Ho \cdot Eu + \frac{1}{Ho} \left(\frac{a_s}{2l_e}\right)^2. \tag{26}$$

For the practical application of equation (26), it is necessary to know the coefficient of hydraulic resistance – the function $\zeta'(t)$ associated with the influence of resistance forces on the flow of the processed medium, the mechanism of action of which is complicated. As a result, in the calculations semi-empirical formulas are used that are valid in particular cases.

According to [14], shut-off valves and regulating devices, which constrict fluid flow, are hydraulically equivalent to the diaphragm. Therefore, to calculate the hydraulic resistance of the modulator RPD, the formulas used to calculate the diaphragms can be used.

Depending on the flow rate, two areas of change in hydraulic resistance can be distinguished (A.D. Altshul formula):

$$\zeta'(t) = \zeta(t) + B(t)/Re, \tag{27}$$

where $\zeta'(t)$ – coefficient of hydraulic resistance in the quadratic domain of dependence of hydraulic losses on the flow velocity;

Re – Reynolds number calculated by the speed in the stator channel;

$B(t)$ – hydraulic loss coefficient determined using reference tables [12] and determining the linear dependence of losses on speed.

The coefficient $\zeta'(t)$ is calculated by the formula

$$\zeta(t) = \left(\frac{S_0}{\varepsilon S(t)}\right)^2, \tag{28}$$

where $S(t)$ – the area of the channel system of the rotor and stator, free for the flow of the processed medium, m².

In the process of opening the stator channel, the processed medium in the RPD chopper accelerates, and its speed increases in the initial time interval, which follows from equation (17), according to the law:

$$v(t) = v(0) + \frac{\Delta P}{\rho l_e} t_0. \tag{29}$$

The linear nature of the function $v(t)$ is preserved for more than half of the expiration period, equal when $a_r = a_s = a$ to $2t_0 = 2a/\omega R_r$ (a_r is the width of the rotor channel). Consequently, considering the nature of the function $v(t)$, the quantity $\Delta Pt_0/\rho l_e$ can be called the average velocity.

The value $\Delta Pt_0/\rho l_e$ is the characteristic speed of a nonstationary flow in RPD and therefore can be chosen as a scale of speed when building similarity criteria for the considered non-stationary hydromechanical process. This value contains information about the parameters of the modulator (t_0, l_0) and medium (ρ). As a time scale, it is advisable to choose a value equal to the half-period of modulation of the velocity and the flow area of the modulator.

With this variant of time and speed, the product of the criteria Eu and Ho is equal to 1 and, therefore, equation (26) is simplified:

$$\frac{dw}{d\tau} + w^2 Ho\zeta(\tau) + wB(\tau) \frac{Ho}{Re} = 1 + \frac{1}{Ho} \left(\frac{a_s}{2l_e}\right)^2. \tag{30}$$

Since the Eu and Ho criteria are independent, any one of them can be applied with equal success. In our case, we use the homochronicity criterion – it is equal to the ratio of the path traveled by the flow at an average speed during the time equal to the half-period of the rotor channel passing through the stator to the length of the liquid column in the modulator, or is the fraction of the liquid column in the RPD modulator leaving the modulator during the half-modulation period.

Denoting the ratio $(ac/2l_e) = Ro$ as a rotation coefficient considering the rotation of the processed medium in the rotor cavity and the associated centrifugal effect, equation (30) of the movement of the treated fluid in the RPD channels will take the form:

$$\frac{dw}{d\tau} + w^2 Ho\zeta(\tau) + wB(\tau) \frac{Ho}{Re} = 1 + \frac{Ro}{Ho}. \tag{31}$$

Introducing the rotational coefficient Ro into equation (31), it is necessary to keep in mind that the centrifugal effect depends not only on the angular velocity of the rotor and its geometrical parameters, but also on the degree of “dragging” the flow into rotational motion, therefore the rotational coefficient should take into account:

$$Ro = \left(a_s/2l_e\right)^2 \cdot K_{rot}, \tag{32}$$

where K_{rot} – coefficient considering the measure of involvement of the flow of the processed medium in the rotational motion. K_{rot} determined experimentally, while $K_{rot} \leq 1$.

In order to solve the nonlinear differential equation (22), it is necessary to know the functions $\zeta(\tau)$ – the coefficient of local hydraulic resistance and $B(\tau)$ – the coefficient of hydraulic resistance, which considers the pressure loss.

In the work [18], using the table of N.E. Zhukovsky (for determining $\zeta(\tau)$) and the table from the reference list of hydraulic resistances [15] (for determining $B(\tau)$), the Runge-Kutta method was used to solve equation (31) for wide intervals changes in the values of the homochronicity criteria, Reynolds criterion, the values of the dimensionless gap, the parameters A and the rotational coefficient Ro :

$$\omega(0) = \frac{-HoB(0)/Re \sqrt{Ho^2 B^2(0)/Re^2 + 4Ho\zeta(0)(1 + Ro/Ho)}}{2Ho\zeta(0)}. \tag{33}$$

The negative root of the quadratic equation is rejected, since the negative velocity (i.e. the flow of fluid towards the pressure drop) is impossible in this situation.



IV. CONCLUSION

The solutions obtained make it possible to determine the influence of various factors on the flow parameters of the treated medium in the rotor and stator channels of the RPD mainly on the acceleration of the fluid, since it is the acceleration that is responsible for the excitation of cavitation in the treated medium.

REFERENCES

1. M. Cvetković, B. Kompare, A.K. Klemenčič, "Application of hydrodynamic cavitation in ballast water treatment". *Environmental Science and Pollution Research*, 2015, 22, pp. 7422-7438.
2. Y.D. Zemenkov, M.Y. Zemenkova, A.A. Vengerov, A.E. Brand, "Application of Technology of hydrodynamic cavitation processing high-viscosity oils for the purpose of improving the rheological characteristics of oils". *IOP Conf. Series: Materials Science and Engineering*, 2016, 154. doi:10.1088/1757-899X/154/1/012026.
3. X. Long, Q. Wang, L. Xiao, J. Zhang, M. Xu, W. Wu, B. Ji, "Numerical analysis of bubble dynamics in the diffuser of a jet pump under variable ambient pressure". *Journal of Hydrodynamics*, 2017, 29(3), pp. 510-519.
4. K.O. Badmus, J.O. Tijani, E. Massima, L. Petrik, "Treatment of persistent organic pollutants in wastewater using hydrodynamic cavitation in synergy with advanced oxidation process". *Environmental Science and Pollution Research*, 2018, 25, pp. 7299-7314.
5. L. Prokhasko, O. Zinina, M. Rebezov, R. Zalilov, Zh. Yessimbekov, I. Dolmatova, Yu. Somova, A. Peryatinskiy, S. Zotov, E. Tumbasova, "Mathematical model of a hydrodynamic cavitation device used for treatment of food materials". *ARPN Journal of Engineering and Applied Sciences*, 2018, 13(24), pp. 9766-9773.
6. V. M. Borisov, A. D. Yatsenko-Zhuk, I.Y. Matyukh, "The prospects of recycling dispersed wastes in rolling and steelmaking industries". *Steel Industry. Bulletin of the Institute "Chermetinform", 1981, 21, pp. 45-59.*
7. S.N. Sirotkin, V.K. Kuznetsov, V.N. Alexandrov, "The rational way of processing and recycling iron-containing wastes of steel industry". *Steel*, 2004, 4, pp. 99-101.
8. Yu.S. Karabasov, Yu.S. Yusfin, I.F. Kurunov, "Environmental problems and technogenic raw materials recycling in steemaking industry". *Steelmaker*, 2004, 8, pp. 27-33.
9. Yu.V. Somova, "Investigation of sludge bottom sediments of steelmaking industry and the technology development of their recycling". *Health Safety in the Third Millennium: Materials of the IV International Research and Practice Conference : in 2 volumes - Chelyabinsk: Publishing Center SUSU*, 2009, 2, pp. 175-182.
10. V. H. Valeev, V.Kh. Valeev, Yu.V. Somova, "Investigation of the mechanical washing process of bottom sediment oily sludge in the terms of hydrodynamic cavitation". *Newsletter of Magnitogorsk State Technical University after G. I. Nosov*, 2012, 3, pp. 55-58.
11. Yu.V. Somova, V.Kh. Valeev, V.D. Cherchintse, "Recycling the Bottom Sediment Oily Sludge of Steelmaking Industry". *Steel*, 2009,3, pp. 86- 87.
12. B.K. Batcha, V. Kirubakaran, "Thermal degradation mechanism of sewage sludge". *ARPN Journal of Engineering and Applied Sciences*, 2018, 13 (24), pp. 9734-9736.
13. Yu.V. Somova, V.Kh. Valeev, M.V. Avdeeva, "Development of the method of oily scale recycling in rolling and steelmaking industries". *Theory and Technology of Steelmaking Industry: Transregional collection of research papers. Magnitogorsk: Publisher: Magnitogorsk State Technical University*, 2007, 7, pp. 150-153.
14. Yu.V. Somova, "Investigation of Hydrodynamic effects on the oily sludge bottom sediments of steelmaking industry". *Scientific Basis and Practice of Processing Ores and Industrial Wastes: The materials of International Scientific and Technical Conference. Yekaterinburg: "Fort Dialog-Iset"*, 2010, pp. 258-262.
15. Yu.V. Somova, V.Kh. Valeev, V.F. Kolesnikov, "Development of the device for selective disintegration of mineral raw materials". *VI Congress of Ore Dressers of CIS Countries: Materials of the Congress. Vol. I. M.: Al'teks*, 2007, pp. 222-234.
16. Yu.V. Somova, "Investigation of Possibility of Using Cavitation Disintegrator for Oily Scale Processing". *Book of Abstracts of International Scientific and Technical Conference of Young Specialists. Magnitogorsk*, 2006, pp. 118-119.
17. N. Muratzhankyzy, A. Kassenov, M. Kakimov, D. Orynbekov, Z. Moldabayeva, Z. Tokhtarov, Z. Yessimbekov, "Mathematical modeling of the relationship between separation and yield of meat-bone scraps in the pressing process". *International Journal of Mechanical Engineering and Technology*, 2018, 9 (9), pp. 968-971.
18. J. Lober, B. Peng, M. Bourassa, J.A. Kozinski, "Pilot-scale direct recycling of flue dust generated in electric stainless steelmaking". *Iron and Steelmaker*, 2000, 1, pp. 41-45.
19. F.R. Young "Cavitation". London, U.K.: Imperial College Press, 1999, 418 p.
20. T.G. Leighton "The Acoustic Bubble" London, U.K.: Academic Press, 1994, 240 p.
21. K.S. Suslick "The chemical Effects of Ultrasound". *Scientific American*, 1989, 2, pp. 80-86.
22. M.Yu. Ryabchikov, B.N. Barankin, S.M. Andreev, P.G. Pol'ko, O. S Logunova, E. S. Ryabchikova, N.A. Golovko, "Fuzzy ekstremalnoe managing the process of grinding ore for maximum performance", *Bulletin of Magnitogorsk State Technical University. G. I. Nosov*, 2011, 4, pp. 65-69.
23. M.Yu Ryabchikov, B.N. Barankin, S.M. Andreev, O.S. Logunova, E. S. Ryabchikova., N.A. Golovko, P.G. Polko, "Achievement of maximum productivity of optimized ore grinding using the principles of fuzzy extreme control". *Newsletter of Magnitogorsk State Technical University after G. I. Nosov*, 2011, 2, pp. 5-9.
24. O.S. Logunova, N.S. Sibileva, V.V Pavlov, "Intellectual Support in Structuring Batch within an Arc Furnace". *Steel in Translation*, 2016, 46(10), pp.733-738.
25. I. Zykova, M. Rebezov, N. Maksimiuk, N. Kuramshina, "The interaction of metals with humic acid of activated sludge and biological treatment facilities sludge", *International Journal of ChemTech Research*, 2016, 9 (3), pp. 372-378.
26. Yu. Somova, E. Degodia, M. Gladysheva, T. Zueva, A. Peryatinskiy, O. Ilyina, G. Valyaeva, A. Yaroslavtsev, A. Pelageina, M. Rebezov, "Sludge deoiling of bottom sediments laboratory installation for carrying out automated scientific research". *International Journal of Mechanical Engineering and Technology*, 2018, 9(5), pp. 498-505.