BER Analysis of MIMO-OFDM System using Different Equalization Techniques under Multipath Fading Channels for Different Modulations

Jagdish Patel, Rana Mahajan, Manohar Wagh

Abstract:- With the rapid growth of digital communication in recent years, the need for high speed data transmission is increased. OFDM is a promising solution for achieving high data rates in mobile environment, due to its resistance to ISI, which is a common problem found in high speed data communication. A multiple-input multiple-output (MIMO) communication System combined with the orthogonal frequency division multiplexing (OFDM) modulation technique can achieve reliable high data rate transmission over broadband wireless channels. MIMO-OFDM system has been currently recognized as one of the most competitive technology for 4G mobile wireless systems. In this paper we discuss the BER performance of the MIMO-OFDM system with two different equalizers (ZF and MMSE) for various modulation techniques i.e. BPSK, QPSK, 16-QAM and 64-QAM using multipath fading channels i.e. AWGN (Additive White Gaussian Noise), Rayleigh and Rician channel. The simulation results show that, with MMSE and ZF equalizers, the BER performances is better in MMSE equalizer. Further we analyzed in different fading channels for various modulation techniques in both the equalizers.

Keywords:- MIMO, OFDM, ZF and MMSE Equalizer, Multipath fading channels, M-QAM

I. INTRODUCTION

Orthogonal frequency division multiplexing (OFDM) is based on multicarrier communication techniques. The idea of multicarrier communications is to divide the total signal bandwidth into number of sub carriers and information is transmitted on each of the sub carriers. Unlike the conventional multicarrier communication scheme in which spectrum of each sub carrier is non-overlapping and band pass filtering is used to extract the frequency of interest, in OFDM the frequency spacing between sub carriers is selected such that the sub carriers are mathematically orthogonal to each others. The spectra of sub carriers overlap each other but individual sub carrier can be extracted by base band processing. This overlapping property makes OFDM more spectral efficient than the conventional multicarrier communication scheme.

As the demand for high-data rate multimedia grows, several approaches such as increasing modulation order or employing multiple antennas at both transmitter and receiver have been studied to enhance the spectral efficiency [1],[2].

II. MIMO-OFDM

OFDM System Model: Figure 1 represents the basic-block diagram of OFDM [4][5] system, consist of transmitter and receiver two sections, named OFDM transceiver system. The data bits inserted from the source are firstly mapped (BPSK, QPSK, 16-QAM, 64-QAM) using given modulation techniques and after that converted from serial to parallel through convertor. Now N subcarriers are there and each sub-carrier consists of data symbol X(k) (k=0,1,…,N-1), where k shows the sub-carrier index. These N subcarriers are provided to inverse fast Fourier transform (IFFT) block. After transformation, the timedomain OFDM signal at the output of the IFFT [5][6] can be written as:

\[ r(n) = \sum_{k=0}^{N-1} X(k) \exp\left(\frac{2\pi i kn}{N}\right) \quad , \quad 0 \leq n \leq N-1 \]  

(1)

MIMO-OFDM (multiple input multiple output orthogonal frequency division multiplexing), a new wireless broadband technology, has gained great popularity for its capability of high rate transmission and its robustness against inter-symbol interference and other channel impairments. Motivated by two vital goals: high-data-rate and high performance. This combination of MIMOOFDM is a very promising feature since OFDM able to sustain of more antennas since it simplify equalization in MIMO systems. Usually in OFDM, fading is considered as a problem in wireless network but MIMO channels uses the fading to increase the capacity of the entire communication network.

Further, this signal model is transformed into a linear form suitable for Zero-Forcing Equalization (linear detection technique), and Minimum Mean Square Error estimation algorithms. MMSE has been shown to perform much better than ZF but more complex than ZF. We can use optimal low rank MMSE estimator to reduce complexity. And finally we can conclude that MMSE is an optimal channel estimator in the sense of achieving the minimum BER.

The organization of the paper is as follows. Section II and III describe the system models of MIMO-OFDM systems and channel estimation respectively. Section IV describe signal detection techniques and in section V we derive the BER performances using both the equalizers for different modifications under multipath fading channels and simulation results are presented in Section VI Conclusion is given in Section VII.

Manuscript Received on December 2014.

Jagdish Patel, Department of Electronics and Telecommunication Engineering Sandip Institute of Technology and Research centre, Nashik (MH)

Rana Mahajan, Department of Electronics and Telecommunication Engineering Sir Vithalbhai Patil Institute Of Technology, Nashik (MH)

Manohar Wagh, Department of Electronics and Telecommunication Engineering Sandip Institute of Technology and Research centre, Nashik (MH)
BER Analysis of MIMO-OFDM System using Different Equalization Techniques under Multipath Fading Channels for Different Modulations

After that, Cyclic Prefix (CP) [7] is added to mitigate the ISI effect. We get signal $x_{cp}(n)$, which is sent to parallel to serial converter again and then, this signal is sent to frequency selective multi-path fading channels [5][8] and a noisy channel with i.i.d. AWGN noise. We used three fading channels in the paper i.e. AWGN, Rayleigh and Rician [8]. The received signal can be given by

$$y_g(n) = x_g(n) * h(n) + w(n), \quad 0 \leq n \leq N - 1 \quad (2)$$

Where $w(n)$ i.i.d. additive white Gaussian noise sample and $h(n)$ is the discrete time channel impulse response (CIR). At the receiver, firstly serial to parallel conversion occurs and cyclic prefix removed. After removing the CP, the received samples are sent to a fast Fourier transform (FFT) block to demultiplex the multi-carrier signals. Then the output of the FFT [5] in frequency domain signal on the kth receiving subcarrier can be expressed as:

$$Y(k) = \frac{1}{N} \sum_{n=0}^{N-1} y(n) \exp\left(-j2\pi kn/N\right) = X(k)H(k) + W(k), \quad 0 \leq k \leq N - 1 \quad (3)$$

where $W(K)$ is noise in time domain and $H(K)$ is the channel frequency response

MIMO System Model: In MIMO system there is a channel/path between each of the transmitters and each of the receiver antennas [9]. If well spacing is there between the transmitting and the receiving antennas, then we achieved sufficiently uncorrelated received signals.

Let us assume a MIMO system with NT transmit antennas and NR receive antennas as shown in figure 2. For simplicity we consider only flat fading; i.e., the fading is not frequency selective, then a matrix of dimension $NT \times NR$ with complex transfer factors $H_{i,j}$ can easily express the channel behavior.

$$[H] = \begin{bmatrix} H_{1,1} & H_{1,2} & \cdots & H_{1,NT} \\ H_{2,1} & H_{2,2} & \cdots & H_{2,NT} \\ \vdots & \vdots & \ddots & \vdots \\ H_{NR,1} & H_{NR,2} & \cdots & H_{NR,NT} \end{bmatrix} \quad (4)$$

Here $H$ is the channel matrix and it is also known as the channel transfer function.

If $X$ represents the vector consisting of the streams transmitted from the transmitting antennas and $R$ represents the received signal vector, then the transmitted samples go through the multipath channel and would reach at the receiver. This could be represented as,

$$R = HX + n \quad (5)$$

Where $n$ is the noise of the same size as $R$ with zero mean and variance $\sigma_d^2$ (white noise) and $X$ is $1 \times NT$ vector and $y$ is $NR \times 1$ vector.

III. CHANNEL DESCRIPTION

We choose three most widely used channels in our paper: AWGN, Rayleigh and Rician fading channels.

**AWGN Channel:** Additive white Gaussian noise (AWGN) channel is a basic or commonly used channel model for analyzing modulation schemes. In this model, the AWGN channel adds a white Gaussian noise to the signal that passes through it. This implies that the channel’s amplitude frequency response is flat (thus with unlimited or infinite bandwidth) and phase frequency response is linear for all frequencies so that modulated signals go through it without any amplitude loss and phase distortion. Fading does not exist for this channel. The transmitted signal gets distorted only by AWGN process AWGN channel is a standard channel used for analysis purpose only.

The mathematical expression in receiving signal is:

$$r(t) = s(t) + n(t) \quad (6)$$

that passes through the AWGN channel where $s(t)$ is transmitted signal and $n(t)$ is background noise or additive white Gaussian noise [10].

Rayleigh Channel: The effects of multipath embrace constructive and destructive interference, and phase shifting of the signal. This causes Rayleigh fading. There is no line of sight (NLOS) path means no direct path between transmitter and receiver in Rayleigh fading channel [9]. The received signal can be simplified to:

$$R(n) = \sum h(n, \tau)S(n - m) + w(n) \quad (7)$$

Where $w(n)$ is AWGN noise with zero mean and unit variance, $h(n)$ is channel impulse response i.e.
\[ h(n) = \sum \alpha(n) e^{-j\theta(n)} \quad (8) \]

Where \( \alpha(n) \) and \( \theta(n) \) are attenuation and phase shift for \( n \)th path.

If the coherence bandwidth of the channel is larger than signal bandwidth, the channel is called flat; otherwise it is frequency-selective fading channel. In this paper, MIMO OFDM is simulated under frequency-selective fading channel.

The Rayleigh distribution [11] is basically the magnitude of the sum of two equal independent orthogonal Gaussian random variables and the probability density function (pdf) given by:

\[ p(z) = \frac{1}{\sqrt{2\pi \sigma^2}} e^{-\frac{z^2}{2\sigma^2}}, \quad z \geq 0 \quad (9) \]

where \( \sigma^2 \) is the time-average power of the received signal and eq. (9) is called a Rayleigh random variable.

**Rician Channel:** In environments where there is a dominant Line-of-Sight (LOS) path between the transmitter and the receiver, the complex Gaussian distributed fading coefficient should be modeled with a non-zero mean, giving rise to the Rician fading. Or also say that, Rayleigh fading with a strong line of sight (LOS) content is said to have a Rician distribution, or to be Rician fading. The Rician distribution is usually characterized by the Rice factor \( \kappa \).

\[ \kappa = \frac{m}{2\sigma^2} \quad (10) \]

which shows the relative strength of the direct LOS path component of the fading coefficient. When \( \kappa = 0 \) this model reduces to Rayleigh fading and as \( \kappa \to \infty \) the fading becomes deterministic giving grow to an AWGN channel.

**IV. SIGNAL DETECTION OF MIMO-OFDM SYSTEM**

MIMO-OFDM detection methods consist of linear and nonlinear detection methods. We are using only linear detection methods in this paper.

Zero Forcing Equalizer: This is a linear equalization algorithm used in communication systems, which inverts the frequency response of the channel at the receiver to restore the signal before the channel [12]. ZF algorithm considers as the signal of each transmitting antenna output as the desired signal, and consider the remaining part as a disturbance, so the mutual interference between the different transmitting antennas can be completely neglected. ZF equalizers ignore the additive noise and may considerably amplify noise for channels with spectral nulls. Mathematical expression of sub-channel in the MIMO-OFDM system is as follows:

\[ R(k) = H(k) X(k) + n(k) \quad (11) \]

Where, \( R(k) \), \( X(k) \) and \( n(k) \) respectively expresses output signal, the input signal and noise vector of the \( K \) sub-channels in MIMO-OFDM system. The relation between input \( X(K) \) and output signal \( R(K) \) as in eq. 11 exploits that this is a linear equalizer.

A ZF detection algorithm for MIMO OFDM is the most simple and basic algorithm, and the basic idea of ZF algorithm is kept of MIMO-channel interference by multiplying received signal and the inverse matrix of channel matrix. Zero-Forcing solution of MIMO-OFDM system is as follows:

\[ X_{ZF} = H^{-1} R = x + H^{-1} n \quad (12) \]

in which \( H^{-1} \) is the channel matrix for the generalized inverse matrix.

**Minimum mean square error (MMSE) equalizer:** A MMSE estimator is a method in which it minimizes the mean square error (MSE), which is a universal measure of estimator quality [12]. The most important characteristic of MMSE equalizer is that it does not usually eliminate ISI totally but instead of minimizes the total power of the noise and ISI components in the output.

Let us assume that \( x \) be an unknown random variable and \( R \) be a known random variable, then

\[ R = HX + n \]

An estimator \( \hat{x} \) (\( R \)) is any function of the measurement \( y \), and its mean square error is given by

\[ MSE = E\{ (\hat{X} - X)^2 \} \quad (13) \]

Where the expectation is taken over both \( X \) and \( R \). The MMSE always performs better than the ZF equalizer and is of the same complications of implementation.

**V. BIT ERROR RATE (BER) AND SIGNAL TO NOISE RATIO (SNR)**

In digital transmission, the no. of bit errors is the number of receiving bits of a signal data over a communication channel that has been changed because of noise, noise, distortion, interference or bit synchronization redundancy.

The bit error rate or bit error ratio (BER) is defined as the rate at which errors occur in a transmission system during a studied time interval. BER is a unit less quantity, often expressed as a percentage or 10 to the negative power.

The definition of BER can be translated into a simple formula:

\[ BER = \frac{number\ of\ errors}{total\ number\ of\ bits\ sent} \]

Noise is the main enemy of BER performance. Quantization errors also reduce BER performance, through unclear reconstruction of the digital waveform. The precision of the analog modulation/ demodulation process and the effects of filtering on signal and noise bandwidth also influence quantization errors.

The SNR is the ratio of the received signal power over the noise power in the frequency range of the process. SNR is inversely related to BER, that is high BER causes low SNR. High BER causes an increase in packet loss, enhance in delay and decrease throughput. SNR is an indicator usually measures the clarity of the signal in a circuit or a wired/wireless transmission channel and measure in decibel...
BER Analysis of MIMO-OFDM System using Different Equalization Techniques under Multipath Fading Channels for Different Modulations

(dB). The SNR is the ratio between the wanted signal and the unwanted background noise

\[ SNR = \frac{P_{signal}}{P_{noise}} \quad (14) \]

SNR formula in terms of diversity: \( BER \propto \frac{1}{SNR d} \quad (15) \)

VI. SIMULATION RESULTS & DISCUSSION

Simulation parameters chosen are listed in Table 1.

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Modulation</td>
<td>BFSK, QPSK, 16QAM, 64QAM</td>
</tr>
<tr>
<td>Channel model</td>
<td>AWGN, Rayleigh, Rician</td>
</tr>
<tr>
<td>Noise model</td>
<td>i.i.d. AWGN</td>
</tr>
<tr>
<td>FFT &amp; IFFT Point</td>
<td>64</td>
</tr>
<tr>
<td>Sub-carrier</td>
<td>52</td>
</tr>
<tr>
<td>Number</td>
<td></td>
</tr>
<tr>
<td>Used sub-carrier</td>
<td>{-26 to -1, +1 to +26}</td>
</tr>
<tr>
<td>CP Length</td>
<td>16</td>
</tr>
<tr>
<td>OFDM symbol length</td>
<td>4( \mu )s</td>
</tr>
</tbody>
</table>

Table-1: Simulation Parameters for MIMO OFDM

In this section simulation results are shown by using two equalizers (ZF and MMSE) in MIMO OFDM system. Various fading channels i.e. AWGN, Rayleigh and Rician fading channels have been determined for different modulation techniques i.e. BFSK, QPSK, 16-QAM and 64-QAM. We analyze the BER performance of data transmission for BFSK, QPSK, 16-QAM and 64-QAM in Matlab software.

Graphs 3, 4 and 5 present the BER values as a function of varying SNR for the MIMO-OFDM system for the ZF equalizer with AWGN, Rayleigh and Rician channels respectively. Through all of the graphs we analyzed that the BFSK modulation gives the least bit error rate, means it is an effective method for data transmission in all of the modulations and for all the channels in terms of bit error rate. For BFSK at the BER value of 10^{-4} we get SNR value of 9.5 dB for AWGN channel in graph 3, 6.75 dB for Rayleigh and Rician channel in graph 4 and graph 5. It represents that Rician and Rayleigh channel behaves similar and better than AWGN channel.
According to the simulation parameters, we can get the following conclusions: BER is clearly low for BPSK, so this is the best modulation technique for data transmission on all the channels used and also for both the equalizers.

Comparing with BPSK modulation, 64-QAM, then 16-QAM and then the QPSK modulation is more sensitive to fading for MMSE equalizer. But for ZF equalizer, when comparing with BPSK modulation, 16-QAM, then 64-QAM and then the QPSK modulation is more sensitive to fading. And also MMSE equalizer outperforms ZF equalizer.

Further work can be extended with other channels i.e. Nakagami-m channels and with different higher order modulation techniques. Also performance can be evaluated using other novel equalizers.

VII. CONCLUSION

According to the simulation parameters, we can get the following conclusions: BER is clearly low for BPSK, so this is the best modulation technique for data transmission on all the channels used and also for both the equalizers. Comparing with BPSK modulation, 64-QAM, then 16-QAM and then the QPSK modulation is more sensitive to fading for MMSE equalizer. But for ZF equalizer, when comparing with BPSK modulation, 16-QAM, then 64-QAM and then the QPSK modulation is more sensitive to fading. And also MMSE equalizer outperforms ZF equalizer.

REFERENCES


