

# Mining Functional Dependency from Relational Databases by Removing Redundant Candidates

Anupama A Chavan, Vijay Kumar Verma

**Abstract**— Discovery of functional dependencies from relational data base has been identified as an important database analysis technique. In this paper, we present a new approach for finding functional dependencies from large databases, based on partitioning the set of rows with respect to their attribute values. The discovery of functional dependencies is easy and efficient due to use of partitions, and the wrong or exceptional rows can be recognized easily. By using this we can eliminate equivalence attribute and redundant dependency. For standard databases the running times are better by several orders of degree over previously published results. The proposed algorithm is also works well for larger datasets than the previous methods.

**Index Terms**— Functional dependencies, closure of set, redundancy, normalization

## I. INTRODUCTION

Normalization is the process of redesigning the database scheme to make it free from all anomalies [12]. Need of normalization is to get a good database design. The problems that occur with bad database design in the relational database are redundancy, updation anomaly, insertion anomaly, deletion anomaly. Repetition of information is called as redundancy which also leads to database inconsistency. Normalization breaks unstructured relation into smaller separate relations and then each individual relation is in normalized form. The idea behind decomposition is to eliminate redundant data and reduce data anomaly. There are many different levels of normalization depending on the purpose of database designer [3] Redundancy is often caused by functional dependency. A functional dependency is a link between two sets of attributes in a relation. We can normalize a relation by removing unwanted FDs. Functional dependencies are relationships between attributes of a relation; a functional dependency states that the value of an attribute is uniquely determined by the values of some other attributes. Automated database analysis is, of course, interesting for knowledge discovery and data mining (KDD) purposes and functional dependencies have applications in the areas of database management, reverse engineering and query optimization. [10]

## II. BASIC CONCEPTS

### A. Functional Dependency

Given a relation 'R', attribute 'Y' of 'R' is functional dependant on attribute 'X' of 'R' if- each 'X' value of 'r' is associated with precisely one value of 'Y' in 'R' .

A functional dependency is a statement  $X \rightarrow Y$  requiring that X functionally determines Y. For example city  $\rightarrow$  state i.e. the state value depends on city value. [7, 8]

#### Properties of Functional Dependency

- Let X and Y be candidates over a dataset D, if  $X \rightarrow Y$  and  $Y \rightarrow X$  hold, then X and Y are said to be equivalent candidates, denoted as  $X \leftrightarrow Y$ .
- Let X, Y and Z are candidates over D. If  $X \leftrightarrow Y$  and  $XW \rightarrow Z$  hold, then  $YW \rightarrow Z$  holds.
- Let X, Y and Z be candidates over D. If  $X \leftrightarrow Y$  and  $WZ \rightarrow X$  hold, then  $WZ \rightarrow Y$  holds.
- Let F be a set of FDs over a dataset D and X be a candidate over D. The Closure of candidate X with respect to F, denoted  $Closure(X)$ , is defined as  $\{Y \mid X \rightarrow Y \text{ can be deduced from F by Armstrong's axioms}\}$ . The nontrivial closure of candidate X with respect to F, denoted  $Closure'(X)$ , is defined as  $Closure'(X) = Closure(X) - X$ .
- Let  $t_1, t_2, \dots, t_n$  be all tuples in a dataset D, and X be a candidate over D. The partition over X, denoted  $|\pi_x|$  is a set of the groups, such that  $t_i$  and  $t_j$  are in the same group if  $t_i[X] = t_j[X]$ . The number of the groups in the partition is called the cardinality of the partition, denoted  $|\pi_x|$ .

### B. Agree Set

Let  $t_i$  and  $t_j$  be tuples and X an attribute set. The tuples  $t_i$  and  $t_j$  agree on X if  $t_i[X] = t_j[X]$ . The agree set of  $t_i$  and  $t_j$  is defined as follows:

$ag(t_i, t_j) = \{A \in R \mid t_i[A] = t_j[A]\}$ . If r is a relation,  $ag(r) = \{ag(t_i, t_j) \mid t_i, t_j \in r, t_i \neq t_j\}$ .

### C. Maximal Set

A maximal set is an attribute set X which, for some attribute A, is the largest possible set not determining A. We denote by  $max(dep(r), A)$  the set of maximal sets for A [4].

## III. PREVIOUS RELATED WORK

In 1999 Yka, Juha, Pasi and Hannu presented "TANE", an efficient algorithm for finding functional dependencies from large database. To test the validity of FDs fast this algorithm is based on partitioning the set of rows with respect to their attribute values. TANE first makes use of partition method and equivalence class.[10].

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In 2000 St\_ephane Lopes, Jean-Marc Petit, and Lot\_Lakhal proposed a new efficient algorithm called Dep-Miner for discovering minimal non-trivial functional dependencies from large databases.[8] N. Novelli and R. Cicchetti, in 2001 proposed FUN: An Efficient Algorithm for Mining Functional and Embedded Dependencies. FUN describes FD approach at a general level only without detailing the optimizations due to the stripped partition database. Concept of free set is used for deriving FDs in this algorithm. [9]

In 2002 Hong Yao and Hamelton and But proposed "FD\_Mine" algorithm. This algorithm needs three procedure one to discover Fd\_Set other to discover EQ\_Set and Prune Candidates and generate next level. Again in 2008 Hong Yao and Hamelton proposed an efficient rule discovery algorithm, called "FD\_Mine", for mining functional dependencies from data by exploiting Armstrong's Axioms for functional dependencies.[6,7]. In 2008 Jalal Atoum, Dojanah Bader and Arafat Awajan proposed a new algorithm FD\_Discover to discover FDs which utilizes the concepts of equivalent properties and minimal (Canonical) cover of FDs. The aim of this algorithm is to optimize the time requirements. [5]

In 2010 Y.V.Sreevani, Prof. T. Venkat Narayana Rao proposed Identification and Evaluation of Functional Dependency Analysis using Rough sets for Knowledge Discovery. A decision table based on certain factors and circumstances related to the knowledge base or the domain is used to discover the dependency between any subset of attributes using rough sets [4]. In 2011 Nittaya Kerdprasop and Kittisak Kerdprasop proposed Functional Dependency Discovery via Bayes Net Analysis. Proposed technique is based on the structure analysis of Bayesian network or Bayes net [3].

IV. DEP-MINER ALGORITHM

St\_ephane Lopes, Jean-Marc Petit, and Lot\_Lakhal in 2000 proposed a new efficient algorithm called Dep-Miner. Dep-Miner is used for discovering agree sets, maximal sets, left-hand sides of minimal non-trivial functional dependencies and real-world Armstrong relations. In Dep-Miner the underlying idea is based on the concept of agree set, which groups all attributes having the same value for a given pair of tuples. Consider the simple employee database as shown in the below table.

I. Simple Employee Database

T No	Emp_No	Dep_No	Year	Dep_Name	Mgr_no
	A	B	C	D	E
1	1	1	2005	Production	5
2	1	5	2004	Marketing	12
3	2	2	2002	Sales	2
4	3	2	2008	Sales	2
5	4	3	2008	Purchase	2
6	5	1	1995	Production	5
7	6	5	1998	Marketing	12

So if we consider employee database given in table 1 maximal equivalence class is

$$MC = \{ \{1,2\}, \{1,6\}, \{2,7\}, \{3,4,5\} \}.$$

For building agree sets, we only consider couples of tuples belonging to a common equivalence class of MC. In our

example the agree set for the pair of tuples(1,2) is  $ag\{A\}$  Similarly we have  $ag(1,6)$ ,  $ag(2,7)$   $ag(3,4) = \{B\_D\_E\}$   $ag(3,5)=\{E\}$   $ag(4,5)=\{C,E\}$ ,so agree sets of r are  $ag(r)=\{A,BDE, E,CE\}$ .

In Dep\_Miner the underlying idea is based on the concept of agree set, which groups all attributes having the same value for a given pair of tuples. From these sets, maximal sets we can derive. The maximal sets for some attribute A are the largest possible sets of attributes not determining A. Then from the complements of these maximal sets they derive the lefthand sides of FDs using a levelwise algorithm for each attribute A it searches for lefthand sides X by increasing the size of X. The only step that requires accessing the database (or rather the stripped partition database) is the computation of agrees sets. This avoid computing agree sets for all pairs of tuples by limiting themselves to the tuples within MC\_ the set of maximal equivalence classes of the stripped partition database  $MC = \max \subseteq \{c \in \pi \mid \pi \in r\}$ ,  $MC = \{ \{1,2\}, \{1,6\}, \{2,7\}, \{3,4,5\} \}$ . An attribute A is included in the agree set of tuples  $\{t_1,t_2\}$  if  $t_1$  and  $t_2$  belong to the same equivalence class in the stripped partition  $\pi_A$ . In our example the agree set for the pair of tuples(1,2) is  $ag\{A\}$  Similarly we have  $ag(1,6)$ ,  $ag(2,7)$   $ag(3,4) = \{B\_D\_E\}$   $ag(3,5)=\{E\}$   $ag(4,5)=\{C,E\}$ ,so agree sets of r are  $ag(r)=\{A,BDE, E,CE\}$ .

The maximal sets from the agree sets as follows, for an attribute A the maximal set  $\max(A, r) = \max \subseteq \{X \in ag(r) \mid A \notin X\}$ . In this example, we have  $\max(A, r)=\{BDE,CE\}$  and the complement of the maximal set of A is  $c\max\{A, r\}=\{AC, ABD\}$ . The complete working process of Dep\_Miner is shown in the table 2. [8]

II. Working of Dep-Miner Algorithm

RHS	cmax (RHS,r)	Size1		Size2	
		Candidate	Traversal	Candidate	Traversal
A	{AC,ABD}	A,B,C,D	A	BC,BD,CD	BC,CD
B	{BCDE,ABD,ABCD}	A,B,C,D,E	B,D	AC,AE,CE	AC,AE
C	{BCDE,AC,ABCD}	A,B,C,D,E	C	AB,AD,AE,DB,BE,DE	AB,AD,AE
D	{BCDE,ABD,ABCD}	A,B,C,D,E	B,D	AC,AE,CE	AC,AE
E	{BCDE}	B,C,D,E	B,C,D,E	-	-

So final FDs are

$$BC \rightarrow A, CD \rightarrow A, D \rightarrow B, AC \rightarrow B, AE \rightarrow B, AB \rightarrow C, AD \rightarrow C, AE \rightarrow C, B \rightarrow D, AC \rightarrow D, AE \rightarrow D, B \rightarrow E, C \rightarrow E, D \rightarrow E$$

V. PROBLEM STATEMENT

The problem addressed in this paper is to find functional dependencies among attributes in a database relation by removing redundant attribute. Specifically, we want to improve on previous proposed methods for this problem. Early methods for discovering of FDs were based on repeatedly sorting and comparing tuples to determine whether or not these tuples meet the FD definition.



The disadvantage of this approach is that it does not utilize the discovered FDs as knowledge to obtain new knowledge. If  $A \rightarrow B$  has been discovered, a check is still made to determine whether or not  $AC \rightarrow B$  holds, by sorting on attributes AC and comparing on attribute B. Instead,  $AC \rightarrow B$  can be directly inferred from the previously obtained  $A \rightarrow B$  without sorting and comparing tuples again. This approach is inefficient because of this extra sorting and because it needs to examine every value of the candidate attributes to decide whether or not a FD holds.

Consider the previous example of employee data base shown in table no 1. From the Dep\_Miner and FUN it is clear that functional dependency are generated for employee relational database are

- |                    |                    |                   |
|--------------------|--------------------|-------------------|
| $BC \rightarrow A$ | $AB \rightarrow C$ | $B \rightarrow D$ |
| $CD \rightarrow A$ | $AD \rightarrow C$ | $B \rightarrow E$ |
| $AC \rightarrow B$ | $AE \rightarrow C$ | $C \rightarrow E$ |
| $AE \rightarrow B$ | $AC \rightarrow D$ | $D \rightarrow E$ |
| $D \rightarrow B$  | $AE \rightarrow D$ |                   |

Total dependencies 14 are generated in these dependencies some of the dependencies are redundant dependencies. Like B derives D and D derive B ( $B \leftrightarrow D$ ). So they are equal equivalent ( $B \leftrightarrow D$ ). From the generated dependencies  $AB \rightarrow C$ ,  $AD \rightarrow C$ ,  $B \rightarrow E$ ,  $D \rightarrow E$  are redundant dependencies. Our approach is to remove these redundant dependencies and generate correct minimal dependencies. In the Dep\_Miner algorithm traversal for size one, row for attribute A and B have the similar candidates and also same set of traversal. So we can take only attribute B and D can be deleted and replace attribute D by B. The steps of proposed method in shown in below figure.

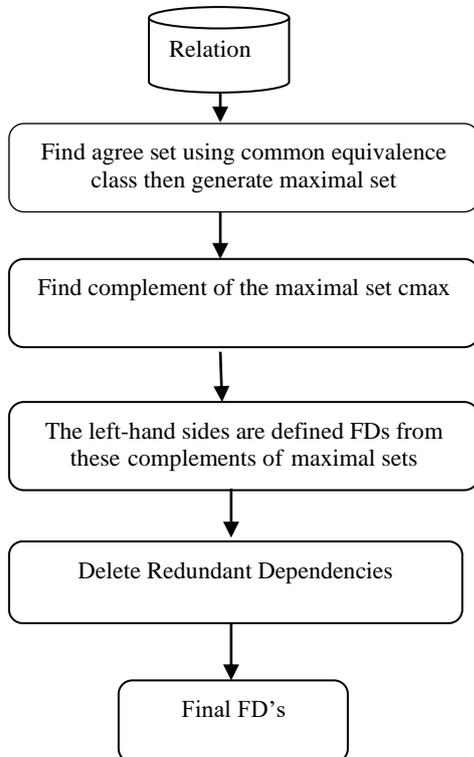


Fig 1-Steps in Proposed Algorithm

The complete working process of the proposed algorithm is shown in below table.

### III. Working of Dep-Miner Algorithm

Now the final functional dependencies are

RHS	cmax(RHS,r)	Size1		Size2	
		Candidate	Traversal	Candidate	Traversal
A	{AC,ABD}	A,B,C,D	A	BC,BD,CD	BC,CD
B	{BCDE, ABD,ABCD}	A,B,C,D,E	B,D	AC,AE,CE	AC,AE
C	{BCDE, AC,ABCD}	A,B,C,D,E	C	AB,AD,AE,D,B,BE,DE	AB,AD,AE
E	{BCDE}	B,C,D,E	B,C,D,E	-	-

- $BC \rightarrow A$     $AB \rightarrow C$     $B \rightarrow E$   
 $CB \rightarrow A$     $AE \rightarrow C$     $C \rightarrow E$   
 $AC \rightarrow B$   
 $AE \rightarrow B$

So there are only 8 functional dependencies are generated.

### VI. ALGORITHM

Discovering minimal functional dependencies

**Input:** a relation r

**Output:** minimal functional dependencies for relation r

1. AGREE SET: computes agree sets from r
2. CMAX SET: derives complements of maximal sets from agree sets
3. LEFT HAND SIDE: computes lhs of functional dependencies from complements of maximal sets
4. DELETE REDUNDANT DEPENDENCIES : find equivalence and remove them also replace deleted attribute by their equivalent
5. FD OUTPUT: outputs functional dependencies

### VII. COMPARISON

We can compare number of dependencies at different level and the comparison chart is shown in the below table.

#### IV. Comparison of Method

Candidate	Dep_Miner	Proposed Algorithm
1	5	2
2	9	6
Total	14	8

The graph also shows the comparison with respect to number of dependencies generated by each of the method.

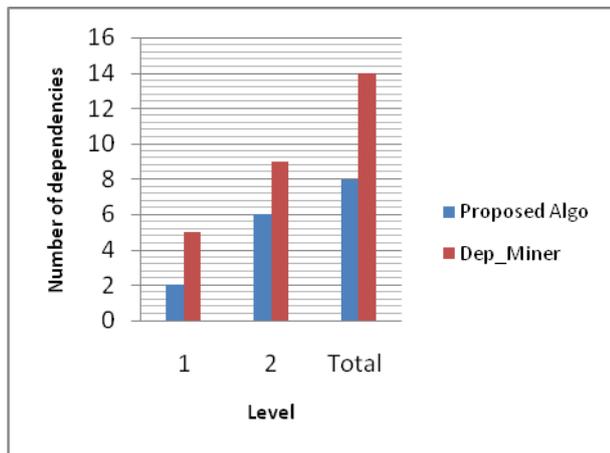


Fig 2-Comparision Graph

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## VIII. CONCLUSION

The main benefit of proposed approach is that the DBA could use functional dependencies for normalizing existing relation schemas and also useful for better understanding relation schemas, and aiding to select only relevant functional dependencies among the whole (and possibly voluminous) set of extracted dependencies. The proposed approach not only reduce extra dependencies but also reduce execution time by deleting equivalence attribute which are unnecessary used in higher level generate. If we delete those attribute earlier then number of candidate at next level will automatically reduce this improves performance of the algorithm.

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