

Comparison of BER of OFDM System using QPSK and 16QAM over Multipath Rayleigh Fading Channel using Pilot-Based Channel Estimation

Sanjay Kumar Khadagade, N.K. Mittal

Abstract– This paper investigate and compare the various channel estimation techniques based on pilot arrangement with the communication system that uses QPSK and 16-QAM to transmit information using OFDM over multipath Rayleigh fading channel. Bit Error Rate (BER) has been considered as the performance index in all analysis. In the block type pilot arrangement, the performance of channel estimation is analyzed with three different algorithms: LS, LMMSE and SVD algorithm. In comb type pilot arrangement, the paper introduces three method of interpolation: linear interpolation, second order interpolation and cubic spline interpolation for channel estimation. The analysis has been carried out with simulation studies under MATLAB environment.

Index Terms- Channel Estimation, OFDM, Pilot Symbol, Rayleigh Fading channel

I. INTRODUCTION

For high-volume and high-speed wireless mobile communication systems, Orthogonal Frequency Division Multiplexing (OFDM) is a promising modulation scheme, and will play an increasingly important role in the future development of wireless mobile communication network due to its high data rate transmission capability with high bandwidth efficiency and its robustness to multi-path delay and no Inter Symbol Interference (ISI). It has been used in wireless LAN standards such as American IEEE802.11a and the European equivalent HIPERLAN/2 and in multimedia wireless services such as Japanese Multimedia Mobile Access Communications.

The channel estimation plays a very important role in OFDM system. For better performance, dynamic estimation of channel is necessary before the demodulation of OFDM signals since the radio channel is frequency selective and time-varying for wideband mobile communication systems [1]. As a research hotpot, many related algorithms have been presented these years, which can be generally separated into two methods, pilot-based channel estimation and blind channel estimation.

Pilot-based channel estimation estimates the channel information by obtaining the impulse response from all

sub-carriers by pilot. Compared with blind channel estimation, which uses statistical information of the received signals, pilot-based channel estimation is a practical and an effective method.

The pilot based channel estimation can be performed by either inserting pilot tones into all of the subcarriers of OFDM symbols with a specific period or inserting pilot tones into each OFDM symbol. The first one, block type pilot channel estimation, has been developed under the assumption of slow fading channel. Even with decision feedback equalizer, this assumes that the channel transfer function is not changing very rapidly. The estimation of the channel for this block-type pilot arrangement can be based on Least Square (LS) or Minimum Mean-Square-Error (MMSE). The MMSE estimate has been shown to give 10–15 dB gain in signal-to-noise ratio (SNR) for the same mean square error of channel estimation over LS estimate [2]. In [3], a low-rank approximation is applied to linear MMSE by using the frequency correlation of the channel to eliminate the major drawback of MMSE, which is complexity. The later, the comb-type pilot channel estimation has been introduced to satisfy the need for equalizing when the channel changes even in one OFDM block. The comb-type pilot channel estimation consists of algorithms to estimate the channel at pilot frequencies and to interpolate the channel. MMSE has been shown to perform much better than LS. In [4], the complexity of MMSE is reduced by deriving an optimal low-rank estimator with singular-value decomposition (SVD). The interpolation of the channel for comb-type based channel estimation can depend on linear interpolation, second order interpolation and spline cubic interpolation. In [4], second-order interpolation has been shown to perform better than the linear interpolation. In [5], cubic spline interpolation has been proven to give lower BER compared to second order interpolation. In this paper, our aim is to compare the performance of all of the above schemes by applying 16QAM (16 Quadrature Amplitude Modulation), QPSK (Quadrature Phase Shift Keying), as modulation schemes with multipath Rayleigh fading and Doppler frequency shift channels with Additive White Gaussian Noise (AWGN) as channel models. In Section II, the description of the OFDM transceiver based on pilot channel estimation, channel modal and QPSK, 16QAM is given. In Section III, the estimation of the channel based on block-type pilot arrangement is discussed. In Section IV, the estimation of the channel at pilot frequencies is presented. In Section VI, the simulation environment and results are described. Section VI concludes the paper.

Manuscript published on 30 February 2013.

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II. SYSTEM MODEL

A. OFDM transceiver

The OFDM system based on pilot channel estimation is given in Fig. 1.

The binary information is first grouped and mapped according to the modulation in “signal mapper.” After inserting pilots either to all sub-carriers with a specific period or uniformly between the information data sequence, IDFT block is used to transform the data sequence of length $N\{X(k)\}$ into time domain signal $\{x(n)\}$ with the following equation:

$$\begin{aligned} \{x(n)\} &= IDFT\{x(k)\}, n=1,2,\dots,N-1 \\ &= \sum_{k=0}^{N-1} X(k)e^{j(2\pi kn/N)} \end{aligned} \quad (1)$$

Where N is the DFT length. We used inverse fast Fourier transform/fast Fourier transform (IFFT/ FFT) in place of IDFT/DFT to reduce computation complexity. Following IDFT block, guard time, which is chosen to be larger than the expected delay spread, is inserted to prevent ISI. This guard time includes the cyclically extended part of OFDM symbol in order to eliminate inter-carrier interference (ICI). The resultant OFDM symbol is given as follows:

$$x_f(n) = \begin{cases} x(N+n), & n = -N_g, -N_g + 1, \dots, -1 \\ x(n), & n = 0, 1, \dots, N-1 \end{cases} \quad (2)$$

Where N_g is the length of the guard interval. The transmitted signal $x_f(n)$ will pass through the frequency selective time varying fading channel with additive noise. The received signal is given by:

$$y_f(n) = x_f(n) \otimes h(n) + w(n) \quad (3)$$

where $w(n)$ is AWGN and $h(n)$ is the channel impulse response. The channel response $h(n)$ can be represented by [5]:

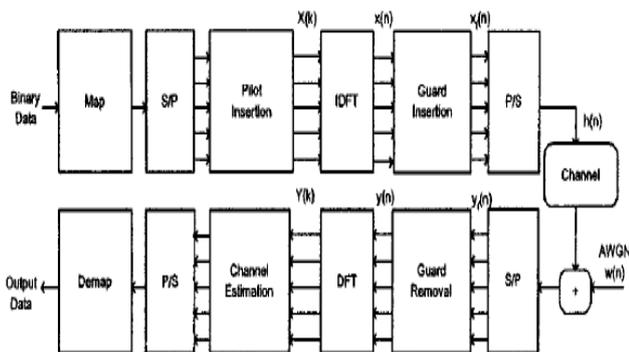


Fig.1. OFDM system for simulation [1].

$$h(n) = \sum_{i=0}^{r-1} h_i e^{j(2\pi/N)f_{Di}T_n} \delta(\lambda - \tau_i), \quad 0 \leq n \leq N-1 \quad (4)$$

where r is the total number of propagation paths, h_i is the complex impulse response of the i^{th} path, f_{Di} is the i^{th} path Doppler frequency shift, λ is delay spread index, T is the sample period and τ_i is the i^{th} path delay normalized by

the sampling time. At the receiver, after passing to discrete domain through A/D and low pass filter, guard time is removed:

$$\begin{aligned} y_f(n) &\quad \text{for } -N_g \leq n \leq N-1 \\ y(n) &= y_f(n + N_g) \quad n = 0, 1, 2, \dots, N-1. \end{aligned} \quad (5)$$

Then $y(n)$ is sent to DFT block for the following operation:

$$\begin{aligned} Y(k) &= DFT\{y(n)\} \quad k = 0, 1, 2, \dots, N-1. \\ &= \frac{1}{N} \sum_{n=0}^{N-1} y(n)e^{j(2\pi kn/N)}. \end{aligned} \quad (6)$$

Assuming there is no ISI shows the relation of the resulting $Y(k)$ to $H(k) = DFT\{h(n)\}$, $I(k)$ that is ICI because of Doppler frequency and $w(k) = DFT\{w(n)\}$, with the following equation [4]:

$$Y(k) = X(k)H(k) + I(k) + W(k), k = 0, 1, \dots, N-1 \quad (7)$$

where

$$\begin{aligned} H(k) &= \sum_{i=0}^{r-1} h_i e^{j\pi f_{Di}T \frac{\sin(\pi f_{Di}T)}{\pi f_{Di}T}} e^{-j(2\pi\tau_i/N)k}, \\ I(k) &= \sum_{i=0}^{r-1} \sum_{\substack{K=0, \\ K \neq k}}^{N-1} \frac{h_i X(K)}{N} \frac{1 - e^{j2\pi(f_{Di}T - k + K)}}{1 - e^{j(2\pi\pi/N)(f_{Di}T - k + K)}} e^{-j(2\pi\tau_i/N)K}. \end{aligned}$$

Following DFT block, the pilot signals are extracted and the estimated channel $H_e(k)$ for the data sub-channels is obtained in channel estimation block. Then the transmitted data is estimated by:

$$X_e = \frac{Y(k)}{H_e(k)}, k = 0, 1, \dots, N-1 \quad (8)$$

Then the binary information data is obtained back in “signal demapper” block.

B. Channel Model

In simulation, we take three OFDM channel model: AWGN channel, Rayleigh fading channel and Doppler spread channel model. In a multipath environment, it is reasonably intuitive to visualize that an impulse transmitted from the transmitter will reach the receiver as a train of pulses. When there are large numbers of paths, applying Central Limit Theorem, each path can be modeled as circularly complex Gaussian random variable with time as the variable. This model is called Rayleigh fading channel model. A circularly symmetric complex Gaussian random variable is of the form,

$$Z = X + jY \quad (9)$$

where real and imaginary parts are zero mean independent and identically distributed Gaussian random variables. For a circularly symmetric complex Gaussian random variable Z , Z which has a probability density,

$$E[z] = E[e^{i\theta}Z] = e^{i\theta}E[z] \quad (10)$$

The statistics of a circularly symmetric complex Gaussian random variable is completely specified by the variance, $\sigma^2 = E[z^2]$ Now, the magnitude

$$p(z) = \frac{z}{\sigma^3} e^{-\frac{z^2}{2\sigma^2}} \quad z \geq 0 \quad (11)$$

is called a Rayleigh random variable. This model called Rayleigh fading channel model, is reasonable for an environment where there are large number reflectors. The channel impulse response (CIR) of Rayleigh multipath channel could be expressed as,

$$h(t, \tau) = \sum_{k=0}^{L-1} u_k e^{j\phi_k} \delta(t - \tau_k) \quad (12)$$

where L is the number of multipath, τ_k is delay of the kth path, $u_k e^{j\phi_k}$ is gain coefficient, respectively. For Doppler spread channel CIR is given by,

$$h(t) = ue^{j\phi} e^{j2\pi f_D t} \quad (13)$$

C. M-ary PSK and 16QAM Modulation in OFDM model

The general analytic expression for M-ary PSK waveform is:

$$s_i(t) = A \cos(\omega_c t + \phi_i(t)); \quad i = 0, 1, 2, \dots, M-1 \quad (14)$$

Where $A = \sqrt{\frac{2E_s}{T_s}}$, $\phi = \frac{2\pi m}{M}$, $m = 0, 1, 2, \dots, M-1$

The parameter E_s is symbol energy, T_s is symbol time duration, and $0 \leq t \leq T$. For BPSK modulation, $M=2$, and for QPSK modulation $M=4$, and the modulation data signal shifts the phase of the waveform, $s_i(t)$. The BPSK bandwidth efficiency is 1 bit/Hz, while QPSK bandwidth efficiency is 2 bits/Hz.

16-QAM is a one type of M-ary QAM, where $M = 16$. In 16-QAM modulation scheme we can send ($k = \log_2 M = \log_2 16 = 4$) 4 bit information per symbol. The general analytic expression for M-ary QAM waveform is:

$$s_i(t) = \sqrt{E_{\min}} a_i \cos(2\pi f_c t) + \sqrt{E_{\min}} b_i \sin(2\pi f_c t) \quad (15)$$

$\sqrt{E_{\min}}$ means the energy of symbol with minimum amplitude. $a_i, b_i (i = 1, 2, \dots, M-1)$ are a pair of independent integer numbers that could be determined by constellation.

D. Pilot Arrangement

The pilot channel estimation methods are based on the pilot channel and pilot symbol. However, due to two-dimensional time-frequency structure of OFDM system, pilot symbol assisted modulation (PSAM) is more flexible [6]. The fading channel of the OFDM system can be viewed as a 2D lattice in a time-frequency plane, because signal is transmitted in the fixed position. And the 2D sampling should satisfy the Nyquist sampling theorem in order to eliminate the distortion. So the minimum limit of pilot symbols inserted is decided by Nyquist theorem. From Nyquist theorem, the

interval of time domain N_t and frequency domain N_f should satisfy [7]

$$f_m T N_t \leq 1/2, \quad \text{and} \quad \tau_{\max} \omega_f N_f \leq 1/2$$

Where ω_f is bandwidth of sub-carrier, T is period of signal, τ_{\max} is the maximum multipath time delay and f_m is the maximum Doppler shift.

The two basic channel estimations in OFDM systems, block-type pilot and comb-type pilot, are illustrated in Fig.2. In the block-type pilot channel estimation, we inserting pilot tones into all subcarriers of OFDM symbols with a specific period in time and in comb-type pilot channel estimation, we inserting pilot tones into certain subcarriers of each OFDM symbol, where the interpolation is needed to estimate the conditions of data subcarriers

III. CHANNEL ESTIMATION BASED ON BLOCK-TYPE PILOT ARRANGEMENT

In block-type pilot based channel estimation, OFDM channel estimation symbols are transmitted periodically, in which all sub-carriers are used as pilots. If the channel is constant during the block, there will be no channel estimation error since the pilots are sent at all carriers. The estimation can be performed by using either LS or MMSE [2], [3]. If ISI is eliminated by the guard interval, we write (7) in matrix notation:

$$Y = XFh + W \quad (16)$$

where

$$X = \text{diag} \{ X(0), X(1), \dots, X(N-1) \}$$

$$Y = [Y(0)Y(1)\dots Y(N-1)]^T$$

$$W = [W(0)W(1)\dots W(N-1)]^T$$

$$H = [H(0)H(1)\dots H(N-1)]^T = \text{DFT}_N \{h\}$$

$$F = \begin{pmatrix} W_N^{00} & \dots & W_N^{0(N-1)} \\ \vdots & \ddots & \vdots \\ W_N^{(N-1)0} & \dots & W_N^{(N-1)(N-1)} \end{pmatrix}$$

$$\text{and } W_N^{nk} = \frac{1}{N} e^{-j2\pi(n/N)k}$$

If the time domain channel vector h is Gaussian and uncorrelated with the channel noise W , the frequency domain MMSE estimate of h is given by [3]:

$$H_{MMSE} = FR_{hY}R_{YY}^{-1}Y \quad (17)$$

where

$$R_{hY} = E \{hY\} = R_{hh}F^H X^H$$

$$R_{YY} = E \{YY\} = XFR_{hh}F^H X^H + \sigma^2 I_N \quad (18)$$

are the cross covariance matrix between h and Y and the auto covariance matrix of Y . R_{hh} is the auto-covariance matrix of h and σ^2 represent the noise variance $E \{W(k)^2\}$. The LS estimate is represented by:



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$$H_{LS} = X^{-1}Y, \quad (20)$$

which minimizes $(Y - XFh)^H (Y - XFh)$.

Since LS estimate is susceptible to noise and ICI, MMSE is proposed while compromising complexity. Since MMSE includes the matrix inversion at each iteration, the simplified linear MMSE estimator is suggested in [8]. In this simplified version, the inverse is only need to be calculated once. In [4], the complexity is further reduced with a low-rank approximation by using singular value decomposition.

Assuming the same signal constellation on all tones and equal probability on all constellation points we get,

$$E\{X^H X\} = E\left\{\frac{1}{|X_k|^2}\right\} I$$

and average Signal to Noise Ratio (SNR) is $\overline{SNR} = E\{|X_k|^2\} / \sigma_N^2$, the term $\sigma_N^2 (X^H X)^{-1}$ is the

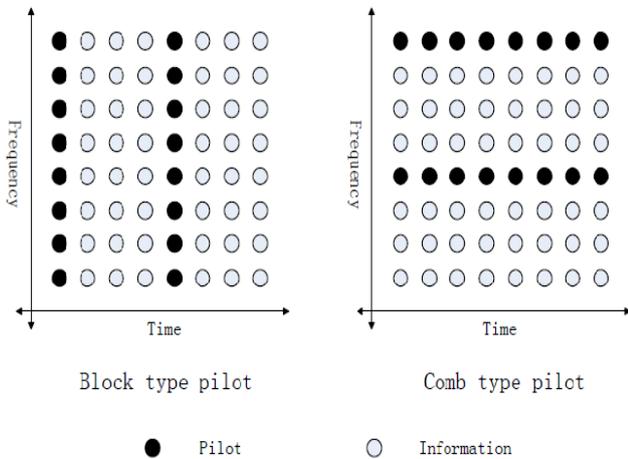


Fig.2. Block type Pilot and Comb type pilot arrangement [2].

approximated by $\frac{\beta}{SNR} I$, where

$$\beta = \frac{E\{|X_k|^2\}}{E\left\{\frac{1}{|X_k|^2}\right\}}. \quad (21)$$

β is a constant which depends only on the signal constellation for QPSK and 16-QAM. Then the modified MMSE estimator in terms of Linear-MMSE is given by:

$$H_{LMMSE} = R_{HH} \left(R_{HH} + \frac{\beta}{SNR} I \right)^{-1} H_{LS}. \quad (22)$$

In [4], the complexity is further reduced with a low-rank approximation by using SVD.

The optimal rank reduction of the estimator in (22), using the SVD, is obtained by exclusion of base vectors corresponding to the smallest singular values [9]. We denote the SVD of the channel correlation matrix:

$$R_{hh} = U \Lambda U^H \quad (23)$$

where U is a matrix with orthonormal columns u_0, u_1, \dots, u_{N-1} and Λ is a diagonal matrix, containing the singular values $\lambda_0 \geq \lambda_1 \geq \dots \geq \lambda_{N-1} \geq 0$, on its diagonal. This allows the estimator in(22) to be written:

$$H_{SVD} = U \Delta U^H H_{LS},$$

where Δ is a diagonal matrix containing the values

$$\delta_k = \lambda_k / \left(\lambda_k + \frac{\beta}{SNR} \right), \quad k = 0, 1, \dots, N-1.$$

on its diagonal. The best rank - p approximation of the estimator in (22) then becomes

$$H_{SVD} = U \begin{pmatrix} \Delta_p & 0 \\ 0 & 0 \end{pmatrix} U^H H_{LS}. \quad (24)$$

where Δ_p is the upper left $p * p$ corner of Δ .

A block diagram of the rank- p estimator in (24) is shown in Fig. 3, where the LS-estimator is calculated from y by multiplying by X^{-1} .

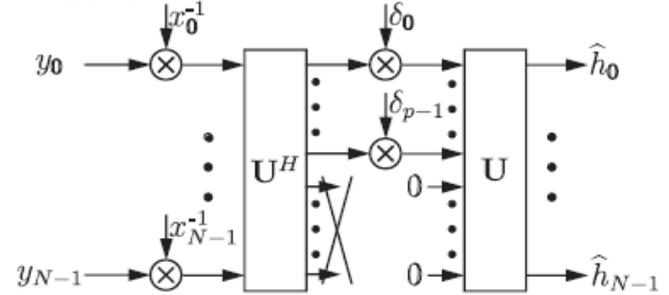


Fig.3 Block diagram of the rank- p channel estimator [3].

IV. CHANNEL ESTIMATION BASED ON COMB-TYPE PILOT ARRANGEMENT

In comb-type pilot based channel estimation, an efficient interpolation technique is necessary in order to estimate channel at data sub-carriers by using the channel information at pilot sub-carriers. Let N_p pilot signals are uniformly inserted into $X(k)$ according to the following equation:

$$X(k) = X(mL + l) = \begin{cases} x_p(m), & l = 0 \\ \text{inf .data} & l = 1, \dots, L-1 \end{cases} \quad (25)$$

where $L = \text{number of carriers} / N_p$ and $x_p(m)$ is the m^{th} pilot carrier value. we define $\{H_p(k), k = 0, 1, \dots, N_p\}$ as the frequency response of the channel at pilot sub-carriers. The estimate of the channel at pilot sub-carriers based on LS estimation is given by:

$$H_e = \frac{Y_p}{X_p} \quad k = 0, 1, \dots, N_p - 1 \quad (26)$$

where $Y_e(k)$ and $X_e(k)$ are output and input at the k^{th} pilot sub carrier respectively.

- The linear interpolation method is shown to perform better than the piecewise-constant interpolation in [9]. The channel estimation at the data-carrier k , $mL < k < (m + 1)L$, using linear interpolation is given by:

$$H_e(k) = H_e(mL + l), \quad 0 \leq l \leq L$$

$$= (H_p(m+1) - H_p(m)) \frac{l}{L} + H_p(m) \quad (27)$$

- The second-order interpolation is shown to fit better than linear interpolation [4]. The channel estimated by second-order interpolation is given by:

TABLE I: SIMULATION PARAMETERS [2].

Parameters	Specification
Channel Bandwidth	1MHz
Number of Sub-Carriers	128
IFFT/FFT size	128 bin points
Pilot Ratio	1/8
Guard Type	Cyclic Extension
Cyclic Prefix Length	16 Samples
Number of Multipath	5
Multipath Delays	0, 2e-6, 4e-6, 8e-6, 12e-6
Sub-Carrier Frequency Spacing	7.8125KHz
Doppler Frequency	40Hz(Block-type), 80Hz(Comb type)

$$H_e(k) = H_e(mL+l) = c_1 H_p(m-1) + c_0 H_p(m) + c_{-1} H_p(m+1) \quad (28)$$

$$\text{where } \begin{cases} c_1 = \frac{\alpha(\alpha-1)}{2}, \\ c_0 = -(\alpha-1)(\alpha+1), \\ c_{-1} = \frac{\alpha(\alpha+1)}{2}. \end{cases} \quad \alpha = \frac{l}{N}.$$

- The cubic spline interpolation is shown to fit better than second-order interpolation [4]. The channel estimated by cubic spline interpola

$$H_e(k) = \alpha_1 H_p(m+1) + \alpha_0 H_p(m) + L\alpha_1 H_p'(m+1) - L\alpha_0 H_p'(m) \quad (29)$$

where $H_p'(m)$ is the first order derivative of $H_p(m)$,

$$\text{and } \begin{cases} \alpha_1 = \frac{3(L-l)^2}{L^2} - \frac{2(L-l)^3}{L^3} \\ \alpha_0 = \frac{3l^2}{L^2} - \frac{2l^3}{L^3} \end{cases}$$

V. SIMULATION

A. System Parameters for Simulation

OFDM system parameters used in the simulation are indicated in Table I: We assume to have perfect synchronization since the aim is to observe channel estimation performance. Moreover, we have chosen the guard interval to be greater than the maximum delay spread in order to avoid inter-symbol interference. Simulations are

carried out for different sig SNR ratios and for different Doppler spreads.

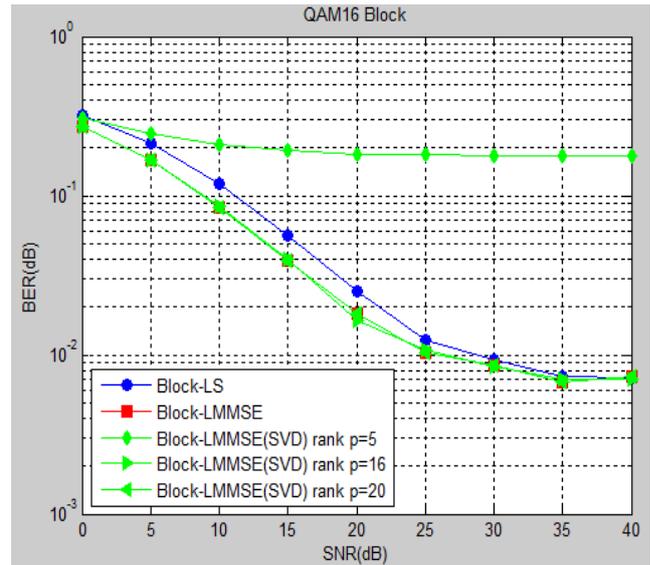


Fig. 4 Comparison of Block type under 16QAM modulation (Doppler frequency=40Hz).

B. Simulation Results

To analyze and compare the performances of different channel estimation schemes for QPSK and 16QAM modulation in OFDM over Rayleigh fading channel, we perform simulation using MATLAB.

Fig. 4 and 6 shows the BER performance of Block type pilot based channel estimation in OFDM system under 16QAM and QPSK modulation respectively, we could find LMMSE with SVD rank p=16,20 have better performance over LS estimator and SVD with rank p=5.

From Fig. 5 and 7 we can see that after performing MATLAB simulation with comb type pilot based channel estimation for 16QAM and QPSK modulation respectively, cubic spline interpolation has better performance over linear and second order interpolation.

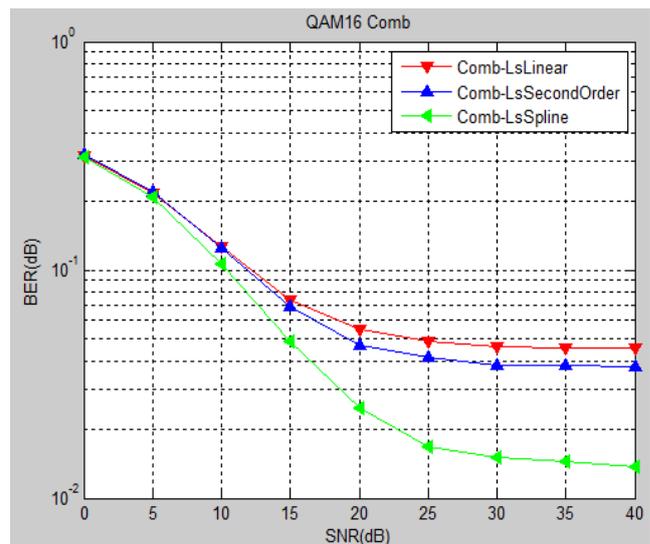


Fig. 5 Comparison of comb type under 16QAM modulation (Doppler frequency=80Hz).

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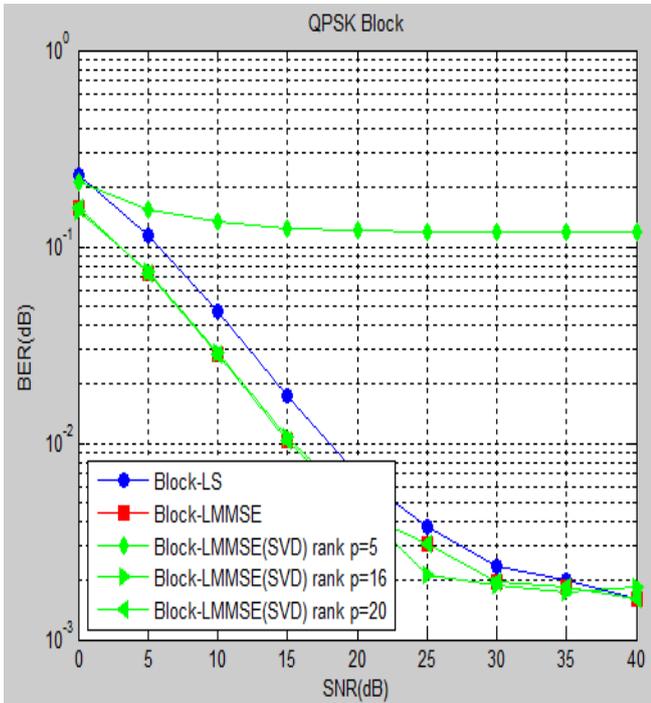


Fig. 6 Comparison of Block type under QPSK modulation (Doppler frequency = 40Hz).

Fig. 8 and 9 shows the comparison between QPSK and 16QAM modulation with Comb type and Block type pilot channel estimation respectively, we could find 16QAM modulation has worse BER performance. But, 16QAM has better bandwidth efficiency. Because 16QAM contains 4 bit information per symbol, and QPSK contains 2 bit information per symbol.

As seen in Fig. 8, the performances of BER for QPSK and 16 QAM with comb-type pilot LS and SVD rank $p=5$ improve but LMMSE and SVD rank $p=16,20$ degraded means comb type pilot based channel estimation used only for fast fading environment with interpolation methods.

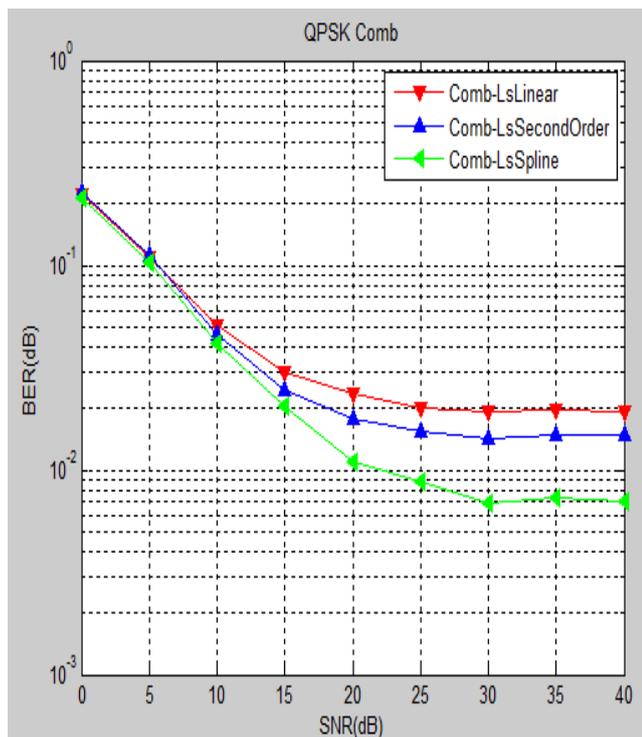


Fig. 7 Comparison of comb type under QPSK modulation (Doppler frequency=80Hz).

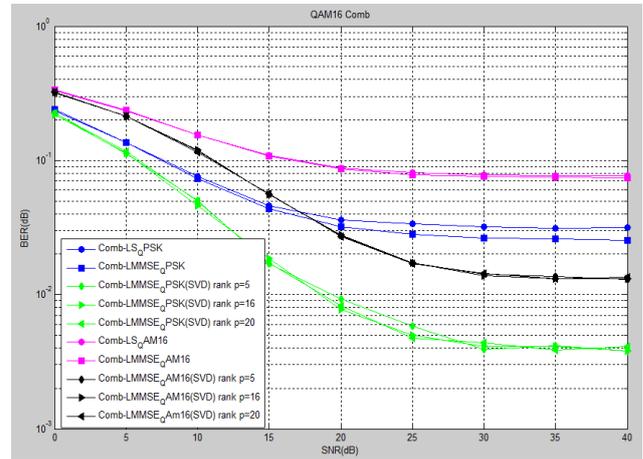


Fig. 8 Comparison of QPSK and 16QAM under comb type pilot (Doppler frequency=80Hz).

Fig. 9 shows the results with Block-type pilot arrangement for QPSK and 16 QAM modulation, we could find that in both cases LMMSE and SVD rank $p=16,20$ have better BER performance.

VI. CONCLUSION

Finally in this paper, we conclude that, in slow fading environment, block type pilot-based channel estimation in OFDM system shows better performance. LS estimator yields the worst performance but with the simplest complexity. Based on LS algorithm, LMMSE is analyzed and it shows better performance compared with LS but with more computation complexity. SVD estimator is further simplification of LMMSE. The simulation results show that SVD estimator has similar performance with LMMSE estimator when p is 16 or larger. In fast fading environment, comb type pilot-based channel estimation in OFDM system has better performance. Linear interpolation, second order interpolation and cubic spline interpolation are discussed. The simulation results show that the performance becomes better as the increasing order of polynomial for interpolation. But the complexity also increases. The effects of using different types of modulation, QPSK and 16QAM, are compared by simulation. 16QAM shows worse performance. However, for the bandwidth efficiency, 16QAM is more feasible in practice.

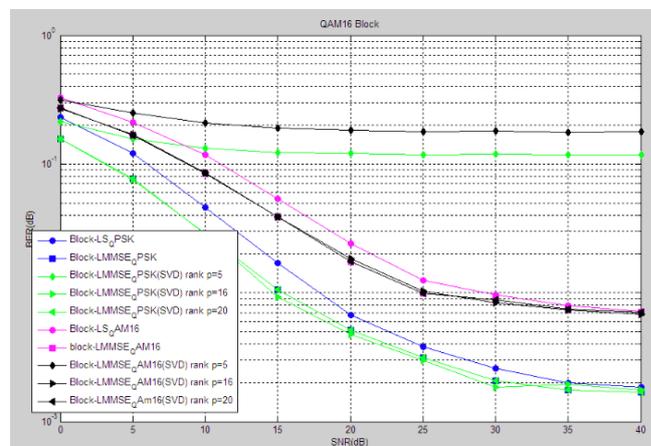


Fig. 9 Comparison of QPSK and 16QAM under Block type pilot (Doppler frequency=40Hz).

REFERENCES

- [1] A. R. S. BAHAI AND B. R. SALTZBERG, *MULTI-CARRIER DIGITAL COMMUNICATIONS THEORY AND APPLICATIONS OF OFDM*, KLUWER ACADEMIC/PLENUM, 1999.
- [2] J.-J. van de Beek, O. Edfors, M. Sandell, S. K. Wilson, and P. O. Borjesson, "On channel estimation in OFDM systems," in *Proc. IEEE 45th Vehicular Technology Conf.*, Chicago, IL, Jul. 1995, pp. 815–819.
- [3] O. Edfors, M. Sandell, J.-J. van de Beek, S. K. Wilson, and P. O. Brjesson, "OFDM channel estimation by singular value decomposition," *IEEE Trans. Commun.*, vol. 46, no. 7, pp. 931–939, Jul. 1998.
- [4] M. Hsieh and C. Wei, "Channel estimation for OFDM systems based on comb-type pilot arrangement in frequency selective fading channels," *IEEE Trans. Consumer Electron.*, vol. 44, no. 1, Feb. 1998.
- [5] R. Steele, *Mobile Radio Communications*. London, England: Pentech Press Limited, 1992.
- [6] R. Van Nee, R. Prasad, *OFDM for Wireless Multimedia Communications*, 1st ed, Artech House, Norwood, MA, 2000.
- [7] P. Hoehner, S. Kaiser, P. Robertson, —Two-dimensional Pilot-Symbol-Aided Channel Estimation by Wiener Filtering, Acoustics, Speech, and Signal Processing, 1997. ICASSP-97., 1997 IEEE International Conference, Apr 1997, Vol. 3, pp. 1845-1848.
- [8] U. Reimers, "Digital video broadcasting," *IEEE Commun. Mag.*, vol. 36, no. 6, pp. 104–110, June 1998.
- [9] Louis L. Scharf. *Statistical Signal Processing: Detection, Estimation, and Time Series Analysis*. Addison-Wesley, 1991.
- [10] M.X.Chang and Yu T.Su , " performance analysis of Equalized OFDM systems in Rayleigh fading" *IEEE Trans. On wireless comm.* Vol. 1 no.4. pp.721-732.oct2002.
- [11] Design and Implementation of Orthogonal Frequency Division Multiplexing by: Alan C. Brooks • Stephen J. Hoelzer.

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