Sliding Mode with Adaptive Control of Robot Manipulator Trajectory Tracking using Neural Network Approximation

Monisha Pathak, Mrinal Buragohain

Abstract: This paper briefly discusses about the Robust Controller based on Adaptive Sliding Mode Technique with RBF Neural Network (ASMCNN) for Robotic Manipulator tracking control in presence of uncertainties and disturbances. The aim is to design an effective trajectory tracking controller without any modelling information. The ASMCNN is designed to have robust trajectory tracking of Robot Manipulator, which combines Neural Network Estimation with Adaptive Sliding Mode Control. The RBF model is utilised to construct a Lyapunov function-based adaptive control approach. Simulation of the tracking control of a 2dof Robotic Manipulator in the presence of unpredictability and external disruption demonstrates the usefulness of the planned ASMCNN.

Keywords: Sliding Mode Control, Robot manipulator, Trajectory Tracking, Neural Network.

I. INTRODUCTION

One of the most prominent intelligent computation systems is the neural network, which has an innate learning capability and can estimate any nonlinear continuing function with precision. Many adaptive neural network control strategy have been created to design robust tracking control of robot manipulators with high nonlinearity using the universal estimation property of many layer neural networks. Sliding mode control (SMC) is one of the most powerful robust non-linear control technique for robot manipulators tracking control in the presence of parametric unpredictability and external disruption [5,6,9]. Sliding mode control necessitates information on the top bound of model unpredictability and external disruptions, and there is always chattering present in practical applications.

Robotic manipulator is a nonlinear, uncertain complex system with unknown dynamics. Designing a robust controller for robot manipulator trajectory tracking is a very challenging task [6]. Uncertainties are always present due to nonlinear frictions and joints flexibility. Many research approaches e.g. Neural network (NN) [1,3,4,15], sliding-mode control [5,9,10], Adaptive control [7], and fuzzy logic [12,14] are available to handle such uncertainties.

In this work a sliding mode with adaptive control based on neural network is designed for trajectory tracking of robot manipulator with modelling uncertainties. The goal is to construct a robust stable controller without using any modelling data. The RBF neural network approximates the unknown nonlinearities in the system and the weight values are adjusted online based on adaptive laws to control the nonlinear system and to have satisfactory tracking of trajectory. The Lyapunov function is utilised to develop the adaptive control law based on the RBF model. The sliding mode function can be thought of as a real-valued effective control, in which the plant performs better when the error is small. The chattering is satisfactorily minimized and the tracking error approaches zero asymptotically.

The following is the breakdown of the paper's structure. The problem is formulated in Section II. In Section III, the ASMCNN controller is designed. Also the stability study of the regulated system is performed in this Section. To validate the control scheme, simulation results conducted on a 2 DOF robotic manipulator are shown in Section IV and conclusions are given in Section V.

II. PROBLEM DESCRIPTION

Let the n-link robot manipulator dynamical equation. ([16]) as

\[ A(q){\ddot q} + C(q, {\dot q}){\dot q} + G(q) + F({\dot q}) + {\tau_d} = {\tau} \]  

(1)

where \( q, {\dot q} \) and \( {\ddot q} \) are vectors of angular position, angular velocity and angular acceleration of the joints respectively. In addition, \( A(q) \) stands for the inertia matrix, \( C(q, {\dot q}) \) stands for the centrifugal Coriolis torque vector. Furthermore, \( G(q) \) stands for the gravitational vector, \( F({\dot q}) \) for friction, \( {\tau} \in {\mathbb{R}}^n \) for joint torque vector, and \( {\tau_d} \) for unknown disturbance.

The dynamical equation of robot manipulator given in (1) has the following properties.

Property I:
The inertia matrix \( A(q) \) is positive definite and symmetric for all \( q \in {\mathbb{R}}^n \), i.e, \( A(q) = {A(q)}^T \) and \( A(q) > 0 \) and it is lower and upper bounded i.e.,

\[ q_1 I \leq A(q) \leq q_2 I \]
\[ m_3 \leq \| A(q) \| \leq m_2 \]  
(2)

where \( q_0 \) and \( q_2 \) are scalar values that may be calculated for any given robot arm. Likewise, the inverse of the inertia matrix is bounded since
\[ \frac{1}{l_2} \leq A(q)^{-1} \leq \frac{1}{l_1} \]  
(3)

Property II:
Matrix \( \hat{A}(q) - 2C(q, \dot{q}) \) is a skew symmetric matrix, i.e.,
\[ x^T \left[ \frac{1}{2} \hat{A}(q) - C(q, \dot{q}) \right] x = 0, \quad \forall x \neq 0 \]  
(4)

**Assumption 1:** The robotic manipulator’s joints are all revolute. Property 1 is valid as a result of this assumption.

**Assumption 2:** \( q, \dot{q} \) and \( \ddot{q} \in \mathbb{R}^n \) are continuous and bounded.

### III. ASMCNN DESIGN AND STABILITY ANALYSIS

The design of ASMCNN is discussed in this section. A trajectory tracking control aim is to design a control torque \( \tau \), for a given desired trajectory \( \dot{q}_d \), the tracking error \( \varepsilon = \dot{q}_d - \dot{q} \) has finite time convergence to zero. Let us define the sliding function as [8]
\[ \sigma = \dot{\varepsilon} - A \dot{\varepsilon} \]  
(5)

where \( \dot{A} = A^T > 0 \), then
\[ \ddot{q} = -\sigma + \dot{q}_d + A \varepsilon \]  
\[ A \ddot{d} = A(\ddot{q}_d - \ddot{q} + A \varepsilon) \]  
\[ = A(\ddot{q}_d + \ddot{\varepsilon}) + C \dot{q} + G + F + \tau_d - \tau \]  
\[ = A(\ddot{q}_d + \ddot{\varepsilon}) - C \sigma + C(\dot{q}_d + A \varepsilon) + G + F + \tau_d - \tau \]  
\[ = -C \dot{\varepsilon} + \tau + \psi + \tau_d \]  
(6)

Where \( \psi(x) = -\dot{\varepsilon} + A \dot{\varepsilon} + C \dot{q} + G + F \) and \( \dot{\varepsilon} = \dot{q}_d + A \varepsilon \) where \( \psi(x) \) contains all the information of modelling. RBFNN is used to approximate \( \psi(x) \). RBFNN algorithm is given as
\[ h_j = \exp \left( \frac{||x - c_j||^2}{\sigma^2} \right), \quad j = 1, 2, \ldots, m \]  
(7)

\[ \psi(x) = Z^T h + \varepsilon \]  
(8)

where \( Z \) is optimum weight value, \( x \) is input of RBFNN, \( h = [h_1, h_2, \ldots, h_m]^T \) and \( \varepsilon \) is a very small number.

The RBFNN output is used to estimate \( \dot{\psi}(x) \).
\[ \ddot{\psi}(x) = Z^T \ddot{h} + \dot{\varepsilon} \]  
(9)

From (7) and (8), we have
\[ \psi - Z^T h + \varepsilon \]  
\[ = Z^T \ddot{h} + \dot{\varepsilon} \]  
\[ = Z^T \ddot{h} + \dot{\varepsilon} \]  
Now from \( \dot{\psi}(x) \), the RBFNN input is chosen as
\[ x = [e^T \quad e^T \quad \dot{q}_d^T \quad \ddot{q}_d^T \quad \dddot{q}_d^T] \]  
\[ \tau = \dot{\psi}(x) + K_r \sigma - \dot{\varepsilon} \]  
(10)

where \( K_r \) is the robust term.

The control law for the system (1) is proposed as
\[ \dot{\varepsilon} = \ddot{\psi}(x) + K_r \sigma - \dot{\varepsilon} \]  
\[ \dot{\varepsilon} = \ddot{\psi}(x) + K_r \sigma - \dot{\varepsilon} \]  
(11)

\[ \ddot{q}_d = \Gamma \ddot{\varepsilon} \]  
where \( \Gamma = \Gamma \ddot{\varepsilon} > 0 \). From (6) yields
\[ \ddot{\varepsilon} = \Gamma \ddot{h} + A \ddot{\varepsilon} + C \dot{\varepsilon} + (\dot{\varepsilon} + A \dot{\varepsilon}) + F \]  
(12)

Consider
\[ \sigma = \sigma(x, \dot{q}_d) + \sigma(\dot{\varepsilon} + \dot{q}_d) + \sigma\dot{\varepsilon} + \sigma \]  
\[ = \sigma\dot{\varepsilon} + \sigma \]  
(13)

Finally yields
\[ \dot{\varepsilon} = -\sigma \ddot{h} \leq 0 \]  
(14)

### IV. SIMULATION RESULTS

Let the n-link robot manipulator dynamical equation as
\[ A(q) \ddot{q} + C(q, \dot{q}) \dot{q} + G(q) + \tau_d = \tau \]  
(15)

\[ A(q) = \begin{bmatrix} m_1 + m_2 + 2m_3 \cos q_2 & m_2 + m_3 \cos q_2 \\ m_2 + m_3 \cos q_2 & m_3 \end{bmatrix} \]  
(16)

\[ C(q, \dot{q}) = \begin{bmatrix} -m_2 \sin q_2 & -m_2 \sin q_2 \\ m_2 \sin q_2 & m_2 \sin q_2 \end{bmatrix} \]  
(17)

\[ G(q) = \begin{bmatrix} m_1 g \cos(q_1 + q_2) \\ m_2 g \cos q_1 \end{bmatrix} \]  
(18)

Let the disturbance \( \tau_d = [0.2 \sin(t) \quad 0.2 \sin(t)]^T \) is added to the system. The frictional force is given as \( F(q) = 0.02 \text{sgn}(q) \). The desired trajectory [9] is
\[ q_{d1} = 1.25 - 1.4e^{-t} + 0.35e^{-3t} \]  
\[ q_{d2} = 1.25 + e^{-t} - 0.25e^{-4t} \]  
(19)

The initial state is
\[ [0.9, 0, -0.09, 0] \]  
(20)

and
\[ m = [m_1, m_2, m_3, m_4, m_5] = [2.9, 0.76, 0.87, 3.04, 0.87] \]  
(21)

\[ z = [\varepsilon \quad \dot{\varepsilon}] \]  
(22)

The following are the control law (19) and adaptive law (20) parameters:
\[ K_r = \text{diag}(20, 20), \Gamma = \text{diag}(17, 17), A = \text{diag}(5, 5) \]  
(23)

The figures 1, 2, 3 and 4 shows the simulation results. Figures show both transient and steadystate characteristics for each joint. Convergence is found satisfactory.
V. CONCLUSION

The Robust Controller based on Adaptive Sliding Mode Control with RBF Neural Network (ASMCNN) for Robot Manipulator trajectory tracking in the presence of unpredictability and disturbances is briefly discussed in this research. The controller is designed with RBF Neural Network estimation without having any modelling information of the plant. The RBF model is utilised to design a Lyapunov function-based adaptive control approach. The chattering action of SMC has been successfully decreased. To validate the designed controller it is successfully employed for tracking control task of a 2dof robot manipulator in presence of uncertainties and disruptions. The tracking error approaches zero asymptotically.

REFERENCES

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